



# Quo Vadis, Britain? – Implications of the Brexit process on the UK’s real economy

Kaan Celebi<sup>1</sup>

Accepted: 6 January 2021 / Published online: 31 March 2021

© The Author(s), under exclusive licence to Springer-Verlag GmbH Germany, part of Springer Nature 2021

## Summary

Using the Panel Data Approach (PDA) of Hsiao et al. *Journal of Applied Econometrics*, 7(5), 705–740 (2012) in combination with the LASSO method, this article aims to measure the effect of the Brexit process on the United Kingdom’s real economy up to 2019Q2. The results are twofold: Firstly, compared to the existing literature, the PDA improves the measurement of the impact of Brexit on the real economy regarding computation intensity, the feasibility of statistical inference and a wider application area. Secondly, the estimated counterfactuals for the UK show that the Brexit process has played a crucial role in the UK’s economy, leading to lower GDP (growth rates), lower private consumption, lower gross fixed capital formation (GFCF) and higher exports. On average, GDP growth has declined between 1.3 and 1.4 percentage points, whereby the cumulative loss ranges between 48 and 54 billion British pounds. Moreover, private consumption in the UK has declined 4.7 billion British pounds quarterly on average. The predicted counterfactuals show that the impact of the Brexit process on GFCF has begun in 2018Q1, whereby the average treatment effect amounts to –2.9 billion British pounds. The UK’s exports increased since the referendum, most likely due to the depreciation of the British pound post-Brexit. The average quarterly effect of the Brexit process on exports is estimated here at 4.8 billion British pounds.

**Keywords** Brexit · Economic policy uncertainty · Counterfactual · Panel data approach · LASSO

**JEL classification** C23 · C54 · E65 · F42 · O47

---

✉ Kaan Celebi  
Celebi@eiiw.uni-wuppertal.de

<sup>1</sup> European Institute for International Economic Relations at the University of Wuppertal, Rainer-Gruenter-Str. 21, D-42119 Wuppertal, Germany

## 1 Introduction

On 23 June 2016, the United Kingdom (UK) voted to leave the European Union (EU). Several years after the referendum, the official British exit, commonly referred to using the portmanteau “Brexit”, took place on 31 January 2020. As of late 2020, the Brexit negotiations between the UK and EU were continuing. The range of possible negotiation results spanned from a hard to a soft Brexit. Both sides are playing the so-called game of chicken (or hawk–dove game) where both maintain a collision course with the other in order to move the negotiating partner toward offering some concessions. Since neither of them is about to swerve and lose the game, the likelihood of a ‘no deal’ Brexit, where both parties lose, has increased during the Brexit process.. Uncertainty about the outcome of the negotiations has resulted in major planning problems in the real sector, since households and companies in the UK are faced with the loss of access to the European Single Market. That is why it is not surprising that the Brexit process itself led to major changes in the economic environment and trade flows of the UK due to the anticipation of the soft or hard Brexit.

Several studies focus on the impact of Brexit on economic factors such as income, welfare, exports, and foreign direct investment (FDI) in the UK, where many contributions employ the gravity model approach. Using a quantitative trade model covering 40 countries and 30 sectors, Dhingra et al. (2017) predict that a soft and a hard Brexit would lead to a fall of the UK’s consumption per capita of about 1.3% and 2.7%, respectively. Furthermore, using a gravity model, they show that the UK’s income per capita declines by between 6.3% and 9.4% due to Brexit. Brakman et al. (2017) use the gravity equation with counterfactual scenarios to analyze the impact of Brexit on exports. By taking 43 countries into account, they show negative trade consequences for both the UK and the EU. Baier and Welfens (2018) examine, using the gravity model, the impact of Brexit on FDI flows and estimate a decline of FDI inflows to the UK by about 42%. Using a panel data structural gravity approach, and assuming different counterfactual post-Brexit scenarios, Oberhofer and Pfaffermayr (2018) find that six years after Brexit occurs, the UK’s (EU’s) exports of goods to the EU (UK) are likely to decline by between 7.2% and 45.7% (or 5.9% and 38.2%). They also find that the UK’s real income is likely to decline by between 1.4% and 5.7% under a hard Brexit scenario and that welfare effects for the EU are insignificant. Henkel and Seidel (2019) run a gravity-spatial model with labour mobility in two counterfactual exercises to study the impact of European integration on welfare and migration flows across 1280 European regions. They estimate welfare losses for the UK of 1.05% and for the EU of 0.41% in the most pessimistic Brexit scenario. Graziano et al. (2018) analyze the uncertainty effects of trade disagreements via a constant elasticity of substitution demand function and find that increasing probabilities of Brexit reduce bilateral export values.

Apart from the gravity model, some studies use program evaluation methodologies, which measure the impact of political or economic interventions by constructing counterfactuals. Usually, a counterfactual without treatment is estimated and compared with the observed series with treatment. In this way the significance and the impact of Brexit can also be measured. Based on Abadie and Gardeazabal (2003), the Synthetic Control Method (SCM) is one of these methodologies. Using the SCM, Douch et al. (2018) estimate the effects on bilateral trade between the UK, on one hand, and 14 EU

and 14 non-EU trading partners, on the other hand, and find that compared with the synthetic UK, exports have declined to both EU and non-EU countries. Serwicka and Tamperi (2018) apply the SCM to examine FDI flows and show that the Brexit referendum reduced the UK's FDI inflows by around 16%–20%. Further recent research about the impact of Brexit on the real economic growth of the United Kingdom is published by Born et al. (2019). Using the SCM, the authors find that by the end of 2018 the gap between the counterfactual and actual GDP ranges between 1.7% and 2.4% of UK GDP and estimate the cumulative loss of the Brexit vote in terms of 2016 GDP at 55 billion British pounds. Moreover, by decomposing real GDP into its components, they find that primarily investments and consumption have been negatively impacted by the Brexit vote.

The main motivation of this paper is to measure the impact of the Brexit process on the real economy. Its primary contribution to the existing literature is in the use of a novel alternative method to the SCM, namely the Panel Data Approach (PDA) of Hsiao et al. (2012). Looking from a different methodological angle, results are obtained which will be compared with previous findings in the literature using SCM. The research mostly relates topically to the study of Born et al. (2019) and analyses the impact of Brexit on real GDP growth, gross fixed capital formation (GFCF), consumption and the export performance of the UK. As proposed by Li and Bell (2017), the PDA is combined with the least absolute shrinkage and selection operator (LASSO) method, which helps to select control units to make adequate out-of-sample predictions.

The results of this research article are twofold. Firstly, from a technically point of view, the PDA appears to be a more appropriate approach in order to measure the impact of Brexit. In contrast to the SCM, the use of the PDA allows to conduct classical inference. Moreover, the PDA approach is able to estimate quantitatively the impact of the Brexit process on consumption and investment, whereas the SCM approach of Born et al. (2019) can only point out the direction of the impact of these variables. This is due to the flexibility of the PDA. In addition to that, the flexibility and the simplicity of the computation of the PDA allow predicting counterfactuals for the UK using a donor pool of countries, whereby member countries of the European Single Market are excluded; indeed excluding major trading partners is adequate in order to avoid having an inadequate donor pool including countries which due to strong trade links partly automatically would lead to a pool of countries with quasi-similarities to the UK simply on the basis of trade links. Since the SCM application of Born et al. (2019) also includes EU countries, which themselves could be significantly affected by the Brexit process, the predicted counterfactuals could be biased due to endogeneity.

Secondly, most of the estimated figures are highly significant and show that, with the exception of UK exports, the Brexit process has been negatively impacting GDP, consumption and GFCF. By 2019Q2, the cumulative loss in terms of UK GDP amounts to between 48 and 54 billion British pounds, whereas the gap between actual output and the counterfactual prediction is approximately 2.5 to 2.7%. The estimated impact on UK exports is positive, most likely because of the depreciation of the British pound following the referendum and during the Brexit process.

The remainder of the paper is organized as follows. Section 2 presents the econometric methodology used, namely the PDA of Hsiao et al. (2012) in combination with the LASSO model selection method. Section 3 describes the data used and the modelling strategy. In Section 4, the empirical results for UK GDP, consumption,

GFCF and exports are presented. Finally, Section 5 provides a summary including policy conclusions. To the best knowledge of the author, studies about the impact of Brexit using this econometric technique and time period do not exist.

## 2 Econometric method

Measuring treatment effects of policy interventions using non-experimental data is a difficult task, since the counterfactual scenario, where no intervention has occurred, is unobservable. In the literature, using the Difference-in-Differences (DID) methodology is one popular way to solve this problem. Nevertheless, the DID method has some urgent limitations regarding the sample selection and statistical behaviour of control and treatment units (Li and Bell 2017, p. 65). To obtain the treatment effect, the SCM compares the treated outcome with randomly matched untreated controls and thus, in contrast to the DID method, is more flexible. In particular, the SCM constructs a counterfactual by calculating a weighted combination of control groups. The objective here is to detect the vector of weights which minimizes the difference between calculated and observed data in the pre-treatment period using covariates between treated and control groups (Gardeazabal and Vega-Bayo 2017, p. 985). The PDA by Hsiao et al. (2012) pursues a similar but more straightforward strategy to calculate counterfactuals. However, the PDA varies from the SCM regarding both the technical focus and the approach (Gardeazabal and Vega-Bayo 2017, p. 987): In the SCM, the counterfactual outcome is predicted using covariates of a panel, whereas the PDA uses only the outcome variable of a panel to construct the prediction. The main idea of the PDA is that a set of common factors, which are the main forces that drive all outcomes of a panel, exists – for example, real GDP. Hence, a factor approach would be able to model the outcome of a unit. Since these factors are not observable, Hsiao et al. propose to use outcomes of the remaining units of a panel in lieu of the common factors in order to model the outcome of the treated unit in the pre-intervention period. Finally, estimated coefficients of the model can be used to construct a counterfactual outcome for the post-intervention period. Besides the simplicity of the computation, the advantage of this approach is the feasibility of significance tests, which is not provided by the SCM.<sup>1</sup>

Let  $\mathbf{y}_t = (y_{1t}, y_{2t}, \dots, y_{Nt})$  represent a vector of panel data across  $N$  countries at time  $t$ . Following Hsiao et al. (2012), the treatment effect for the  $i$ th country at time  $t$  is

$$\Delta_{it} = y_{it}^1 - y_{it}^0 \quad (1)$$

where  $y_{it}^1$  and  $y_{it}^0$  denote the outcome of the  $i$ th country at time  $t$  under treatment and in the absence of treatment, respectively. As mentioned previously,  $y_{it}^1$  and  $y_{it}^0$  cannot be observed simultaneously. This can be formulated as follows:

$$y_{it} = d_{it} y_{it}^1 + (1 - d_{it}) y_{it}^0 \quad (2)$$

<sup>1</sup> In case of the SCM, the probability distribution of the predicted pre-treatment outcome is not easily derivable, so that statistical tests cannot be performed (Hsiao et al. 2012, p. 711).

with

$$d_{it} = \begin{cases} 1, & \text{if the } i\text{th country is under treatment at time } t \\ 0, & \text{otherwise} \end{cases} \tag{3}$$

Suppose the treatment, i.e. the Brexit vote, occurs at time  $T_1$ . Then, the vector of observed outcomes  $\mathbf{y}_t$  before the policy change at  $T_1$  can be noted as

$$\mathbf{y}_t = \mathbf{y}_t^0, \text{ for } t = 1, \dots, T_1 \tag{4}$$

Moreover, suppose that the treatment has an impact only on the first country, i.e. the UK, and thus the outcomes of other units (countries) of the panel are not affected by the treatment:

$$y_{1t} = y_{1t}^1, \text{ for } t = T_1 + 1, \dots, T \tag{5}$$

$$y_{it} = y_{it}^0, \text{ for } i = 2, \dots, N, \text{ for } t = 1, \dots, T \tag{6}$$

Under the assumption that  $K$  common factors drive the outcomes of the panel,  $y_{it}^0$  can be modelled as follows:

$$y_{it}^0 = \alpha_i + \mathbf{b}'_i \mathbf{f}_t + \varepsilon_{it} \text{ with } i = 1, \dots, N, \text{ for } t = 1, \dots, T \tag{7}$$

where  $\mathbf{f}_t$  is the  $K \times 1$  vector of (unobservable) common factors that vary over time,  $\mathbf{b}'_i$  is the  $1 \times K$  vector of constants, which can vary across units  $i$ ,  $\alpha_i$  is the fixed unit-specific intercept and  $\varepsilon_{it}$  is the idiosyncratic error term with  $E(\varepsilon_{it}) = 0$ . This factor model can be stacked together in terms of the  $N$  units:

$$\mathbf{y}_t^0 = \boldsymbol{\alpha} + \mathbf{B} \mathbf{f}_t + \boldsymbol{\varepsilon}_t \text{ for } t = 1, \dots, T \tag{8}$$

where  $\boldsymbol{\alpha}$  contains the  $N \times 1$  vector of individual intercepts,  $\mathbf{B} = (\mathbf{b}_1, \dots, \mathbf{b}_N)'$  denotes the  $N \times K$  factor loading matrix and  $\boldsymbol{\varepsilon}_t$  is the  $N \times 1$  vector of error terms. As is usual in the literature,  $\boldsymbol{\varepsilon}_t$  is assumed to be stationary and with  $E(\boldsymbol{\varepsilon}_t) = 0$ . Furthermore, it is assumed that  $\boldsymbol{\varepsilon}_t$  is homoscedastic and that  $E(\boldsymbol{\varepsilon}_t \mathbf{f}'_t) = 0$ . Hsiao et al. (2012, p. 707) assume, that  $\text{Rank}(\mathbf{B}) = K$  should hold, which implies that  $N$  is greater than the number of common factors ( $K$ ), which is easily satisfied in practice (Li and Bell 2017, p. 67).

Equations (1) and (7) show that for the post-treatment period of the first country, which is the unit affected by the policy change, the outcome can be written as follows:

$$y_{1t} = y_{1t}^1 = y_{1t}^0 + \Delta_{1t} = \alpha_1 + \mathbf{b}'_1 \mathbf{f}_t + \varepsilon_{1t} + \Delta_{1t} \text{ for } t = T_1 + 1, \dots, T \tag{9}$$

The number of common factors  $K$  could be identified using the procedure of Bai and Ng (2002) in order to estimate  $\mathbf{f}_t$ . This holds only for large  $N$  and  $T$ , which are often in

practice not given. Hsiao et al. (2012, p. 709) show that the counterfactual prediction of  $y_{1t}^0$  in the pre-treatment period can be realized by using  $\tilde{\mathbf{y}}_t = (y_{2t}, \dots, y_{Nt})'$ , which are not affected by the policy change but which are affected by the common factors, in lieu of  $\mathbf{f}_t$ :

$$y_{1t}^0 = \bar{\alpha} + \tilde{\mathbf{a}}' \tilde{\mathbf{y}}_t + \varepsilon_{1t}^* \tag{10}$$

where  $\bar{\alpha}$  and  $\tilde{\mathbf{a}}$  denotes the constant and the vector of coefficients, respectively, and  $\varepsilon_{1t}^*$  is the error term. To construct the counterfactual, the following procedure is used by Hsiao et al. (2012):

Step 1:  $y_{1t}^0$  has to be regressed on  $\tilde{\mathbf{y}}_t$  for the pre-treatment period ( $t = 1, \dots, T_1$ ) using eq. (10).

Step 2: The obtained estimates for  $\bar{\alpha}$  and  $\tilde{\mathbf{a}}$  are used to calculate  $\hat{y}_{1t}^0$  for the post-treatment period ( $t = T_1 + 1, \dots, T$ ).

Using  $\hat{y}_{1t}^0$  in eq. 1, the average treatment effect (ATE) can be estimated as follows:

$$ATE = \frac{1}{T-T_1} \sum_{i=T_1}^T y_{1t} - \hat{y}_{1t}^0 = \frac{1}{T-T_1} \sum_{i=T_1}^T \hat{\Delta}_{1t} \tag{11}$$

In the case of stationary  $\hat{\Delta}_{1t}$ , the significance of the treatment effect can be tested by a t-test. If the predicted treatment effect is serially correlated, the inference of ATE can be performed by applying an OLS model with only a constant as independent variable and a heteroskedastic-autocorrelation consistent variance-covariance estimator proposed by Newey and West (1987):

$$\hat{\Delta}_{1t} = \alpha_0 + \hat{\varepsilon}_t \tag{12}$$

where the constant  $\alpha_0$  equates to the ATE. To evaluate the significance of the ATE, a t-test using HAC standard errors can be applied. Moreover, an AR( $p$ ) model can be fit for the estimated treatment effects  $\hat{\Delta}_{1t}$ :

$$\hat{\Delta}_{1t} = \beta_0 + \sum_{i=1}^p \beta_i \hat{\Delta}_{1(t-i)} + \hat{\varepsilon}_t \tag{13}$$

The constant  $\beta_0$  of the AR( $p$ ) fit represents the short-run treatment effect (STE) and can be tested for significance by applying a t-test. Additionally, in the case that AR( $p$ ) is stationary  $\left( \left| \sum_{i=1}^p \beta_i \right| < 1 \right)$  and thus converges towards a steady state, the implied long-run effect (LTE) can be measured as follows:

$$LTE = \frac{\beta_0}{1 - \sum_{i=1}^p \beta_i} \tag{14}$$

By applying a Wald-test, the significance of the LTE can be evaluated.

To perform step 1, a model selection criterion is needed. Hsiao et al. (2012) suggest using the (corrected) Akaike Information Criterion (AIC and AICC) or the Bayesian Information Criterion (BIC) to select the most relevant predictors. The problem of these model selection methods is that in the case of a larger number of countries  $N$  than the pre-treatment sample size  $T_1$ , ordinary least squares (OLS) cannot be applied, which means that the researcher is forced to make preliminary decisions (Li and Bell 2017, p. 66). However, the LASSO method, which shrinks less significant coefficients to zero, provides a model selection method which allows  $N$  to be higher than the sample size (Meinshausen and Yu 2009). Moreover, as shown in Li and Bell (2017, p. 71), the PDA using the LASSO method leads to smaller out-of-sample predictive mean squared errors, smaller computational times and lower numbers of selected regressors compared to the use of AIC, AICC and BIC. It is also shown that, in the case of an increasing  $N$ , AICC tends to select more regressors, whereas the LASSO method provides rather robust numbers of regressors.<sup>2</sup>

Considering the factor model in eq. (10) for the pre-treatment period, the LASSO method solves the following problem to obtain the estimates for  $\bar{\alpha}$  and  $\tilde{\mathbf{a}}$  (Tibshirani 2011, p. 273):

$$\min_{\bar{\alpha}, \tilde{\mathbf{a}}} \left\{ \sum_{t=1}^{T_1} \left( y_{1t}^0 - (\bar{\alpha} + \tilde{\mathbf{a}}' \tilde{\mathbf{y}}_t) \right)^2 + \lambda \sum_{j=1}^N |\tilde{a}_j| \right\}, \tag{15}$$

where  $\tilde{a}_j$  is the  $j$ th element of the coefficient vector  $\tilde{\mathbf{a}}$  and  $\lambda$  is a tuning parameter. In eq. (15) one can see that the first term is the OLS loss function, whereas the second term penalizes the coefficients' size in order to decrease the variance of the estimation. A higher parameter  $\lambda$  increases the penalty on coefficients  $\tilde{a}_j$ , which means that the LASSO procedure shrinks more non-zero and high coefficients  $\tilde{a}_j$  towards zero. This is because higher coefficients lead to an increasing estimation variance and, by extension, to increasing errors, whereby the bias increases (Li and Bell 2017, p. 70). As a result, the LASSO method provides a technique where both the variance of the estimated coefficients  $\left[ \text{Var}(\hat{\mathbf{a}}) \right]$  and the bias of the estimated coefficients  $\left[ E(\hat{\mathbf{a}}) - \tilde{\mathbf{a}} \right]$  are regarded as trade-offs.

In practice, the tuning parameter calibration is solved by using cross-validation (CV) methods (Tibshirani 2011, p. 278). CV is a model validation technique which tests the out-of-sample accuracy of the model. Here, the parameter  $\lambda$  is searched over a discrete

<sup>2</sup> This behaviour of the model selection methods explains the smaller predictive mean squared errors of the LASSO method, since a large number of regressors increases the variance of the estimation leading to poorer predictive accuracy (Li and Bell 2017, p. 69).

set  $A_L = \{\lambda_1, \dots, \lambda_L\}$ . A popular CV method, which Li and Bell (2017, p. 70) propose for the LASSO method, is the leave-one-out (LOO) CV. For each pre-treatment period  $t = 1, \dots, T_1$  and for each element  $\lambda_k (k = 1, \dots, L)$  of  $A_L$  the coefficients  $\bar{\alpha}$  and  $\tilde{\mathbf{a}}$  are estimated by solving the following problem:

$$\min_{\bar{\alpha}, \tilde{\mathbf{a}}} \left\{ \sum_{s=1, s \neq t}^{T_1} \left( y_{1s}^0 - (\bar{\alpha} + \tilde{\mathbf{a}}' \tilde{\mathbf{y}}_s) \right)^2 + \lambda_k \sum_{j=1}^N |\tilde{a}_j| \right\}. \tag{16}$$

As a result of the minimizations, a  $T_1 \times L$  set of coefficients  $\widehat{\alpha}_{-t,k}, \widehat{\mathbf{a}}_{-t,k}$  is estimated, whereby these coefficients are the LOO (leave the  $t$ -th observation out) estimates of  $\bar{\alpha}$  and  $\tilde{\mathbf{a}}$ :

---

	$\lambda_1$	$\lambda_2$	...	$\lambda_L$
$t=1$	$\widehat{\alpha}_{-t=1,k=1}, \widehat{\mathbf{a}}_{-t=1,k=1}$	$\widehat{\alpha}_{-t=1,k=2}, \widehat{\mathbf{a}}_{-t=1,k=2}$	...	$\widehat{\alpha}_{-t=1,k=L}, \widehat{\mathbf{a}}_{-t=1,k=L}$
$t=2$	$\widehat{\alpha}_{-t=2,k=1}, \widehat{\mathbf{a}}_{-t=2,k=1}$	...	...	...
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$
$t=T_1$	$\widehat{\alpha}_{-t=T_1,k=1}, \widehat{\mathbf{a}}_{-t=T_1,k=1}$	...	...	$\widehat{\alpha}_{-t=T_1,k=L}, \widehat{\mathbf{a}}_{-t=T_1,k=L}$

---

In order to obtain  $\lambda$ , for each tuning parameter  $\lambda_k (k = 1, \dots, L)$  the average squared error over all  $T_1$  observations is calculated by using the estimated coefficients  $\widehat{\alpha}_{-t,k}, \widehat{\mathbf{a}}_{-t,k}$  of eq. (16):

$$CV(\lambda_k) = \frac{1}{T_1} \sum_{t=1}^{T_1} \left( y_{1t}^0 - (\widehat{\alpha}_{-t,k} + \widehat{\mathbf{a}}_{-t,k}' \tilde{\mathbf{y}}_t) \right)^2 \text{ for } k = 1, \dots, L. \tag{17}$$

The tuning parameter  $\lambda_k$ , which minimizes  $CV(\lambda_k)$ , is used in eq. (15). Finally, the coefficients of regressors, which the LASSO procedure shrinks to zero, are redundant for the factor model, whereas regressors, whose coefficients are non-zero, are selected as adequate predictors for the PDA.

### 3 Data and Modelling strategy

As mentioned previously, donor countries, which are serving as controls, should not be affected by Brexit. Therefore, several member countries of the European Single Market are excluded. The economic characteristics of donor countries should, as far as is reasonably possible, be similar to those of the UK. For this reason, countries which are covered in the database of the Organisation for Economic Co-operation and Development (OECD), namely all OECD member countries and some selected non-member countries, are considered as controls. As a last step, countries which do not belong to the UK's top 25 export partners of 2015, 2016 and 2017 and which do not have quarterly data

available for a period of about ten years are also excluded.<sup>3</sup> Following these steps, the control countries remaining in the donor pool are: Australia, Brazil, Canada, China, India, Israel, Japan, Korea, Mexico, New Zealand, Russia, Turkey and the United States.

First of all, the LASSO-LOO procedure is used to obtain controls which result in the best (out-of-sample) fit for the pre-treatment period.<sup>4</sup> At this point, the econometric aim is not to deliver an explanatory model but to mimic the pre-treatment period in order to predict the post-treatment counterfactual output. Since economic characteristics, interdependencies and behaviours change over time, the use of recent data should be preferred to predict the current edge adequately. Therefore, for all donor countries and the UK, the following data in national currencies are extracted from the OECD database for the period 2008Q1 to 2019Q2: real GDP growth, GDP, private consumption, GFCF and exports. Table 1 gives an overview of the data used.<sup>5</sup> Since the Brexit referendum took place on 23 June, 2016, 2016Q2 is set as the cut-off point  $T_1$ . As a result, the pre-treatment and post-treatment period covers 34 or 12 observations for each control, respectively.

The prediction of the year-on-year growth rates of consumption, GFCF and exports using control group growth rates is rather difficult. That is why local currency levels of donor countries are used to predict the level for the UK.<sup>6</sup> In these cases, to avoid spurious regressions, the Engle and Granger (1987) single-equation cointegration test is performed, whereby the time series of the UK is used as the dependent variable of the regression. In the event that the LASSO-LOO procedure delivers (non-stationary) controls as predictors, whose linear combinations are not cointegrated, the procedure including the single-equation Engle-Granger test is iteratively repeated. In each iteration, donor countries are removed from the donor pool one-by-one in order to identify those countries which lead to a test statistic failing to reject the null hypothesis of no cointegration. The iteration stops when the LASSO-LOO procedure picks controls which lead to a rejection of the null hypothesis of no cointegration at least at the 10% significance level.<sup>7</sup>

<sup>3</sup> The export ranking of the UK is calculated using the World Integrated Trade Solution (WITS) database of the Worldbank. The exclusion of the member countries of the European Single Market and the consideration of the countries with high foreign trade activity with the British economy serves to prevent endogeneity problems and to estimate the post-treatment period using countries with strong affiliation to the UK economy in order to better reflect relevant shocks stemming from these countries. Nevertheless, as an anonymous referee has pointed out, it is important to be aware that an affiliated country could theoretically be affected from policy changes emanating from the UK. However, the exclusion of any possible endogeneity problems is practically impossible and lies in the “nature” of impact evaluation methods, which is also well-known in the literature (Wan et al. 2018, p.123): “For PDA and SCM to yield reasonable estimates of counterfactuals, the control units must not be affected by the intervention. It could be hard to find a control group that is invariant to such disruptions. For instance, it is not that easy to find control groups to measure the impact of the Iranian revolution on the Iranian economy”.

<sup>4</sup> For the empirical study, the „*lasso*“function of MATLAB R2013b is used. The calibration set  $\lambda_L = \{\lambda_1, \dots, \lambda_L\}$  comprises a geometric sequence with 100  $\lambda$ -variations. The largest number  $\lambda_L$  is set to result the first non-null model, where all coefficients are shrunk to zero.

<sup>5</sup> Descriptive statistics and unit root test result can be found in the Appendix in Tables 13 and 14.

<sup>6</sup> In this article, all figures given in British pound sterling are in terms of 2016.

<sup>7</sup> Cointegration relationships have apparently not been considered in previous empirical applications of the PDA in use of non-stationary variables (see e.g. Ke et al. 2017). In the opinion of the author, this could lead to spurious post-treatment projections. The present modeling strategy tries to avoid such problems and is therefore a more conservative and precautionous implementation of the PDA. As a result, the LASSO is used to enhance the prediction accuracy, whereas the cointegration is checked for non-stationary variables to provide predictors with common stochastic trend.

**Table 1** Donor pool overview

Dependent variable for UK	Real GDP growth*	GDP**	Priv. consumption**	GFCF**	Exports**
Australia	✓*	✓**	✓**	✓**	✓**
Brazil	✓*	✓**	✓**	✓**	✓**
Canada	✓*	✓**	✓**	✓**	✓**
China	✓*	—	—	—	—
India	✓*	✓**	✓***	✓***	✓***
Israel	✓*	✓**	✓**	✓**	✓**
Japan	✓*	✓**	✓**	✓**	✓**
Korea	✓*	✓**	✓**	✓**	✓**
Mexico	✓*	✓***	✓***	✓***	✓***
New Zealand	✓*	✓**	✓**	✓**	✓**
Russia	✓*	✓**	✓**	✓**	✓**
Turkey	✓*	✓**	✓**	✓**	✓**
United States	✓*	✓**	✓**	✓**	✓**

\*y-o-y, SA

\*\*CVM, SA, LC

\*\*\*Constant prices, SA, LC

CVM: chained volume measures; SA: seasonally adjusted; LC: local currency; y-o-y: year-on-year

Data source: OECD database, Quarterly National Accounts

To assess the precision of the estimators, 95% confidence bands for the counterfactual prediction are calculated using the Newey-West HAC variance-covariance estimator.<sup>8</sup>

Since country-specific shocks, particularly in the post-Brexit period, could lead to a bias of the counterfactual prediction, the whole econometric procedure will be repeated by dropping these countries from the donor pool. Possible candidates here are developing countries such as Turkey and Brazil, whose GDP growths were relatively volatile in the last three years.<sup>9</sup>

As mentioned previously, serially correlated treatment effects have to be fitted by an  $AR(p)$  model. To identify the adequate number of lags  $p$ , the Schwarz information

<sup>8</sup> For all HAC estimations the Bartlett kernel density and the lag selection parameter of Andrews and Monohan (1992) are used.

<sup>9</sup> Regarding the post-Brexit referendum period, the standard deviation of the GDP growth of Turkey and Brazil are 4.6 and 1.5 times higher, respectively, than the mean of the standard deviation of the growth rates of the donor pool. Turkey's economy suffered from US sanctions and tariffs in 2018 and also from the offensive into north-eastern Syria in 2019. The recent country-specific political, legal and economic turmoil in Turkey are discussed in Grübler (2017, pp. 11–12). Between 2014 and 2017, Brazil's economy slumped into a recession due to a political crisis, high fiscal deficits and a collapse in commodity and oil prices.

Since remarkable country-specific developments should be excluded as far as possible from the counterfactual prediction, results after these exclusions have been considered more reliable in the subsequent section. It would be not quite surprising, that these exclusions from the donor pool lead to differing results, in particular when crucial country-specific economic developments have taken place in the post-Brexit period. Also for this reason numerical results should be viewed with a certain degree of caution.

criterion (BIC) is used. Since the residuals of the AR(*p*) estimation could still be serially correlated, Newey-West HAC variance-covariance estimators are used for inference.<sup>10</sup>

## 4 Results of the PDA LASSO-LOO approach

### 4.1 Results for GDP growth and GDP level

To quantify the impact of the Brexit-process on real GDP growth, the described econometric approach is applied for three different donor pool compositions. The estimation results are reported in Appendix Tables 2, 3 and 4, whereas Figs. 1, 2 and 3 illustrate the actual and predicted values of the growth rate.<sup>11</sup> In the first estimate, real GDP growth rates of all available donor countries are used in the LASSO-LOO procedure, which picks all controls as regressors in order to construct the counterfactual growth path. Apparently, the actual and the counterfactual growth path diverge in the post-Brexit referendum period. The ATE is -1.00 percentage points and is, according to the t-test with HAC standard errors, significant at the 1 % level. Since the estimated treatment effects are serially correlated, an AR(4) model is fitted:

$$\hat{\Delta}_{1t} = -\frac{1.8292}{(0.0026)} + \frac{0.0110}{(0.9593)}\hat{\Delta}_{1(t-1)} + \frac{0.3170}{(0.3369)}\hat{\Delta}_{1(t-2)} - \frac{0.0789}{(0.8848)}\hat{\Delta}_{1(t-3)} - \frac{0.7453}{(0.0405)}\hat{\Delta}_{1(t-4)} + \hat{\varepsilon}_t \tag{18}$$

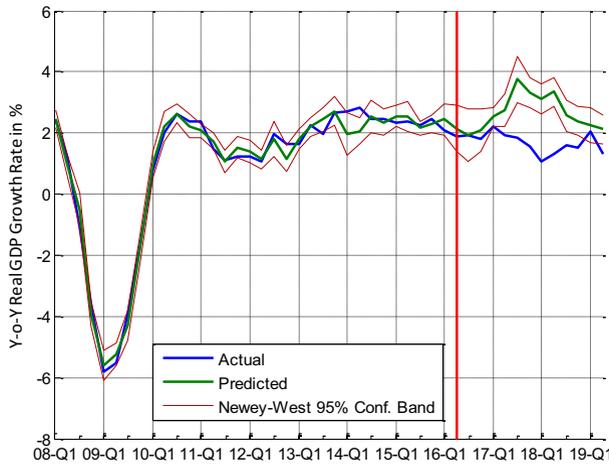
where estimated HAC *p* values are in parentheses. The STE and the LTE are -1.83 and - 1.22 percentage points, respectively, and are significant at the 1 % level. Nevertheless, it is remarkable that at the end of the post-Brexit referendum period actual and predicted growth rates converge.

Considering the discussed country-specific shocks, Turkey is excluded from the donor pool in the second estimate, whereas in the third estimate developing countries like Turkey, Brazil, India and Mexico are excluded. The second and third estimates show similar predictions. A comparison of the first with the second and third estimates implies that the convergence of the actual and predicted path in the first estimate is mainly caused by a country-specific shock in Turkey. The ATEs of the second and third estimate are 1.39 and 1.31 percentage points, respectively, and are both statistically significant at any significance level. The treatment effects of the second estimate are fitted by an AR(1) model:

$$\hat{\Delta}_{1t} = -\frac{0.5970}{(0.1139)} + \frac{0.5912}{(0.0232)}\hat{\Delta}_{1(t-1)} + \hat{\varepsilon}_t \tag{19}$$

<sup>10</sup> As the BIC is known to be very strict in selecting the number of variables to be included, it might also be possible to overcome the problem of the autocorrelation of residuals by including further time lags instead of correcting the variance-covariance matrix. However, due to the closeness of the Brexit vote, the limited number of observations for the post-treatment period may make it difficult to estimate the autoregressive model.

<sup>11</sup> The following Tables of results (Tables 2-12) can be found in the Appendix.



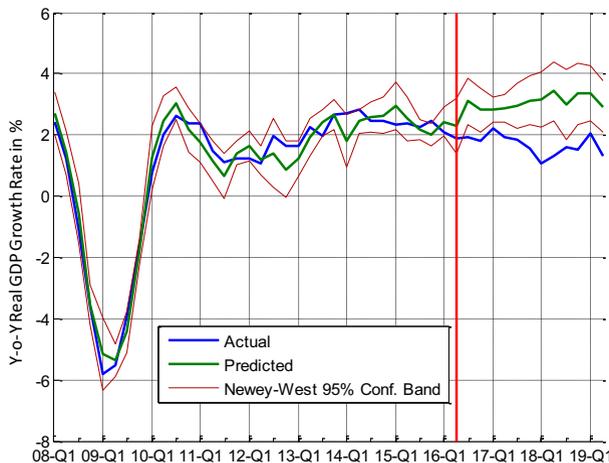
**Fig. 1** The UK’s actual and predicted real GDP growth rates. Prediction computed by using all available donors (first estimate)

The LTE is  $-1.46$  percentage points and, according to the Wald-test, significant at the 1 % level. The treatment effects of the third estimate are also fitted by an AR(1) model:

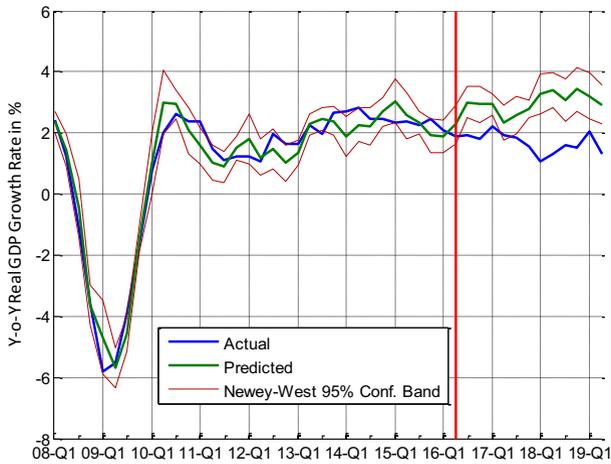
$$\hat{\Delta}_{1t} = -\frac{0.5993}{(0.1239)} + \frac{0.5679}{(0.0154)} \hat{\Delta}_{1(t-1)} + \hat{\varepsilon}_t \tag{20}$$

The LTE is  $-1.39$  percentage points and also significant at the 1 % level.

As described previously, the econometric approach is also applied for GDP in local currency levels. The estimation results are reported in Appendix Tables 5 and 6, whereas Figs. 4 and 5 illustrate the actual and predicted GDP. In the first estimate, where all available controls are used, the LASSO-LOO procedure picks Japan, Korea and the United States as predictors. The



**Fig. 2** The UK’s actual and predicted real GDP growth rates. Prediction computed after removing Turkey from the donor pool (second estimate)

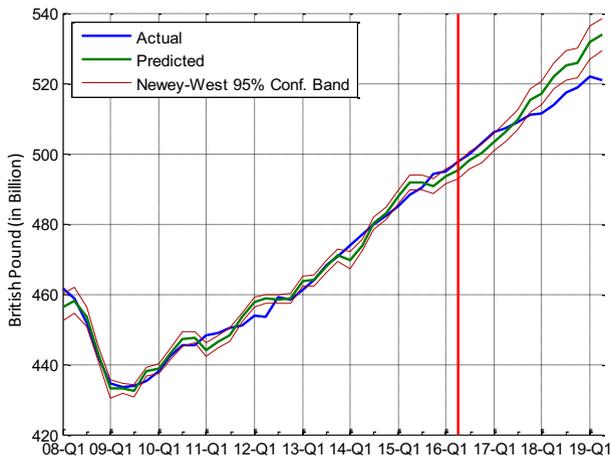


**Fig. 3** The UK’s actual and predicted real GDP growth rates. Prediction computed after removing Turkey, Brazil, Mexico and India from the donor pool (third estimate)

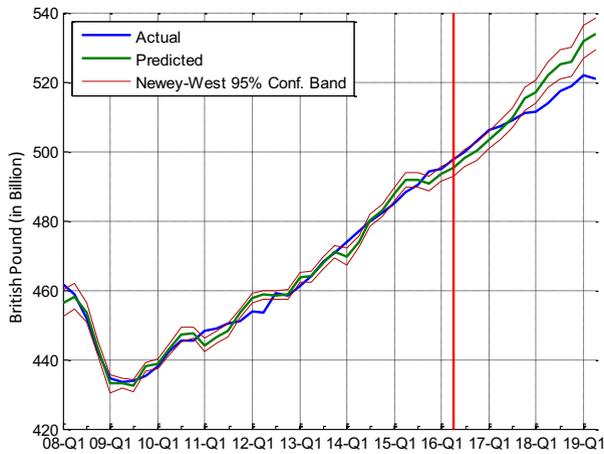
Engle-Granger test shows that the null hypothesis of no cointegration can be rejected with a  $p$  value of 0.0682. The ATE of the first estimate is  $-3.99$  billion British pounds but narrowly misses the 10 % significance level ( $p$  value = 0.12). Due to serial correlation, an AR(2) model is fitted for the treatment effect:

$$\hat{\Delta}_{1t} = \underbrace{-1.3574}_{(0.0091)} + \underbrace{1.2957}_{(0.0004)} \hat{\Delta}_{1(t-1)} - \underbrace{0.3305}_{(0.1618)} \hat{\Delta}_{1(t-2)} + \hat{\varepsilon}_t \quad (21)$$

The STE and the LTE are  $-1.36$  and  $-39.04$  billion British pounds, respectively, and are both significant at the 1 % level. By summing up the differences of actual and



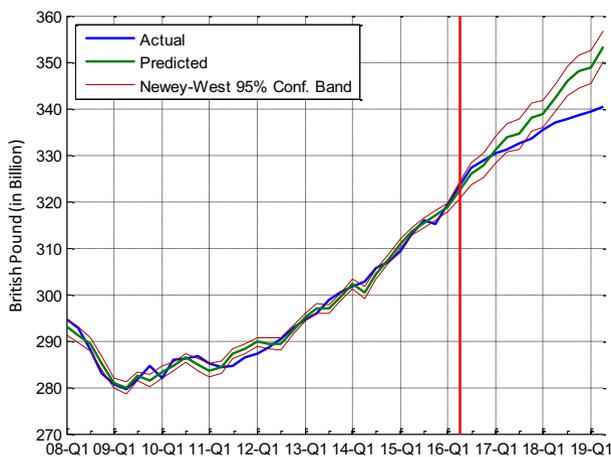
**Fig. 4** The UK’s actual and predicted GDP (in billion British pounds, CVM). Prediction computed by using all available donors (first estimate)



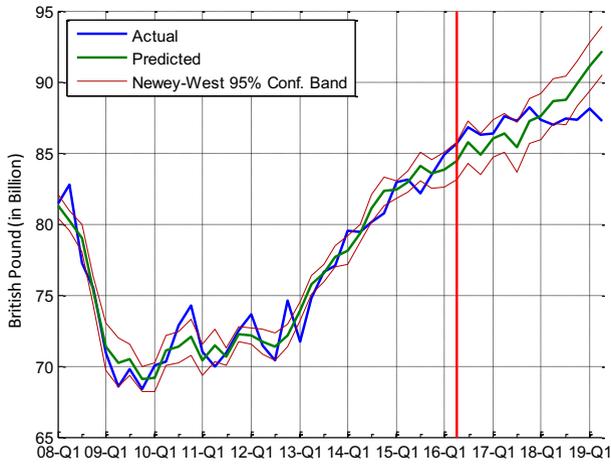
**Fig. 5** The UK’s actual and predicted GDP (in billion British pounds, CVM). Prediction computed after removing Japan from the donor pool (second estimate)

predicted GDP, the cumulative treatment effect of the Brexit-process is approximately  $-48$  billion British pounds.

In the second estimate for GDP, Japan is removed from the donor pool in order to increase the cointegration relationship. Here, the LASSO-LOO procedure picks Australia, Canada, Korea and the United States as predictors. Nevertheless, the Engle-Granger test shows a higher  $p$  value than in the first estimation, namely  $0.09$ . Apart from the weak cointegration, there are fairly stable links between the UK and the predictors of the second estimate, since the LASSO-LOO selects, besides the United States, two Commonwealth countries. The ATE of the second estimate is  $-4.49$  but with a  $p$  value of  $0.12$  is also not



**Fig. 6** The UK’s actual and predicted private consumption (in billion British pounds, CVM). Prediction computed by using all available donors

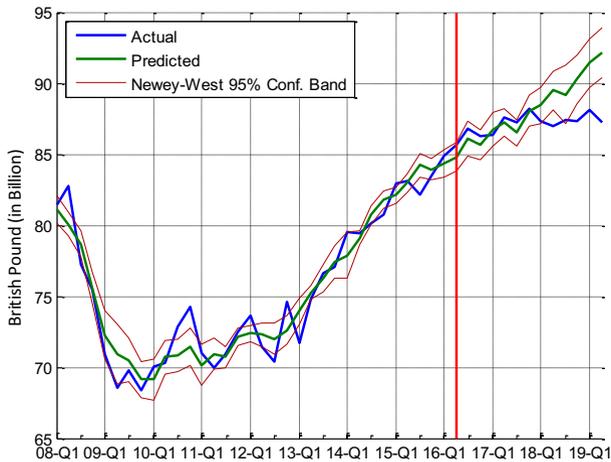


**Fig. 7** The UK’s actual and predicted GFCF (in billion British pounds, CVM). Prediction computed by using all available donors (first estimate)

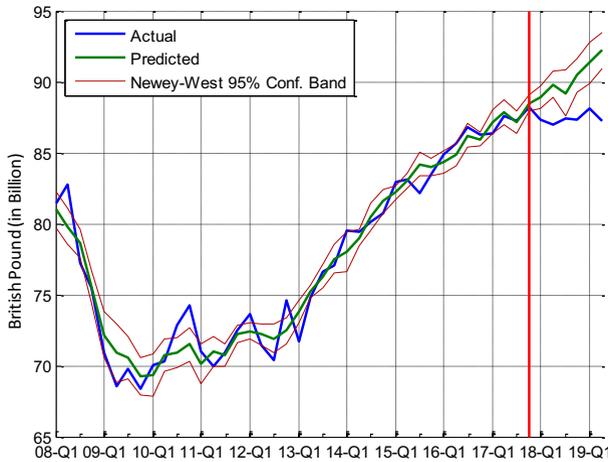
significant at the 10 % level. The treatment effects of the second estimate are also fit to an AR(2) model:

$$\hat{\Delta}_{1t} = \underbrace{-1.3544}_{(0.0041)} + \underbrace{1.3377}_{(0.0000)} \hat{\Delta}_{1(t-1)} - \underbrace{0.3493}_{(0.0286)} \hat{\Delta}_{1(t-2)} + \hat{\varepsilon}_t \quad (22)$$

The STE of the second estimate is also  $-1.36$  billion British pounds and significant at the 1 % level. The LTE in the second estimate is  $-117.1$  billion British pounds and is also significant at the 1 % level. However, it differs strongly from the result in the first estimate, which is due to higher dynamics in the autoregressive representation.



**Fig. 8** The UK’s actual and predicted GFCF (in billion British pounds, CVM). Prediction computed after removing Brazil from the donor pool (second estimate)

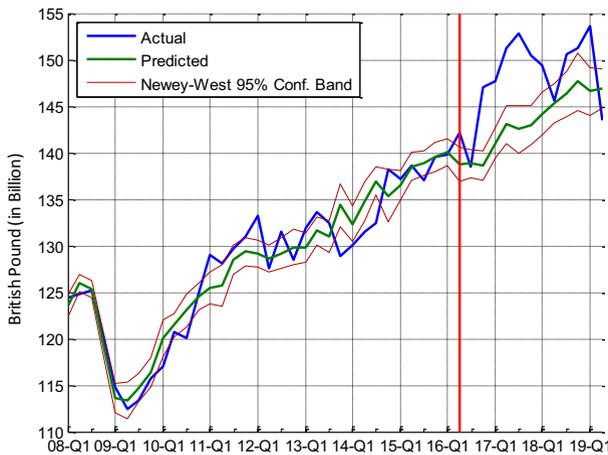


**Fig. 9** The UK’s actual and predicted GFCF (in billion British pounds, CVM). Prediction computed after removing Brazil from the donor pool and with cut-off point 2018Q1 (third estimate)

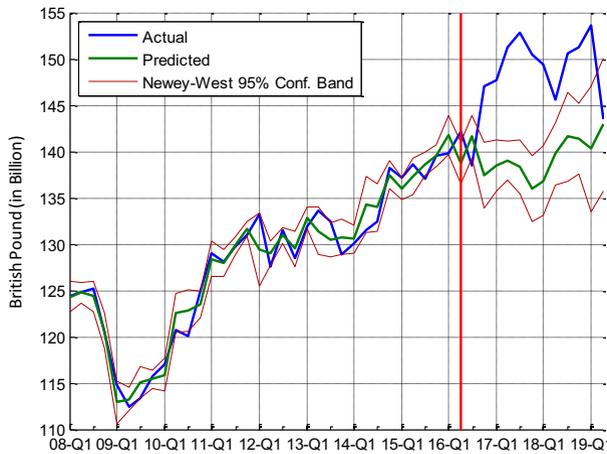
The cumulative loss since the Brexit referendum is approximately 54 billion British pounds.

**4.2 Results for private consumption**

Using private consumption panel data, the LASSO-LOO procedure picks Australia, Japan, New Zealand and the United States as predictors of British private consumption. The  $p$  value of the Engle-Granger test (0.0346) is below the 5 % level and thus indicates the presence of a cointegration relationship. In addition to that, the chosen predictors are, like the UK, developed countries, whereas two of them belong to the group of Commonwealth countries. Regarding these stable links, further estimations



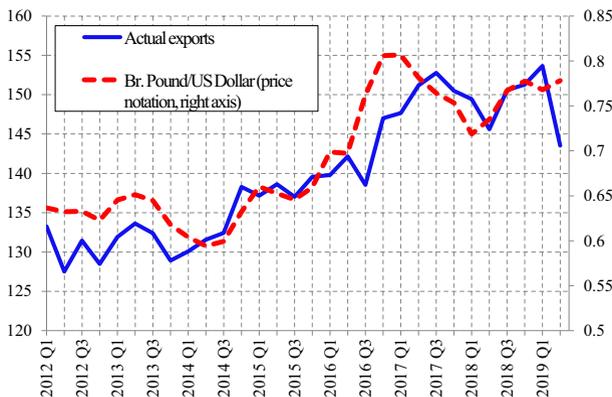
**Fig. 10** The UK’s actual and predicted exports (in billion British pounds, CVM). Prediction computed by using all available donors (first estimate)



**Fig. 11** The UK’s actual and predicted exports (in billion British pounds, CVM). Prediction computed after removing Brazil from the donor pool (second estimate)

have been found unnecessary. Appendix Table 7 summarizes the results for the UK’s private consumption, whereas in Fig. 6 the actual and counterfactual paths are plotted.

At first glance, the changing trend of the actual path in the post-Brexit vote period stands out, whereas the predicted path of private consumption holds the trend of the previous period. As a result, the actual and the predicted consumption path diverge evidently. Regarding the t-statistic using Newey-West standard errors, the ATE on UK’s private consumption, which is  $-4.67$  billion British pounds, is significantly different from zero at the 5 % level. The treatment effects are serially correlated and are fitted using a (non-stationary) AR(2) model:



**Fig. 12** The UK’s exports and the British pound/US dollar exchange rate (price notation). Source: OECD Monthly Monetary and Financial Statistics, own calculations.

$$\hat{\Delta}_{1t} = -\frac{1.7623}{(0.0015)} + \frac{0.4428}{(0.1969)} \hat{\Delta}_{1(t-1)} + \frac{0.6240}{(0.0977)} \hat{\Delta}_{1(t-2)} + \hat{\varepsilon}_t \quad (23)$$

The STE is  $-1.76$  billion British pounds and is statistically significant at the 1 % level. However, the LTE cannot be calculated since the sum of the AR-coefficients is greater than one and thus does not lead to a convergent result due to non-stationary dynamics in the AR-process. For the post-Brexit referendum period, the cumulative treatment effect for the UK's private consumption is approximately 56 billion British pounds.

### 4.3 Results for GFCF

According to the LASSO-LOO procedure using the whole GFCF panel data, the adequate predictors of the UK's GFCF are Australia, Japan, New Zealand, United States and Brazil. Appendix Table 8 outlines the estimation results, whereas Fig. 7 displays the actual and predicted values of the UK's GFCF. Regarding the  $p$  value of the Engle-Granger test (0.0075), the linear combination of the variables used is cointegrated below the 1 % significance level. Apparently, fixed investments are not impacted by the Brexit process until the end of 2017. After 2017Q4, the UK's actual GFCF breaks the trend of the previous periods and proceeded to stagnate, whereas the predicted GFCF holds the trend. As a result, the actual and predicted GFCF begin to diverge starting from 2018Q1.

The ATE is 0.57 billion British pounds and is not significantly different from zero. The treatment effects are serially correlated and thus fit to a (non-stationary) AR(1) model:

$$\hat{\Delta}_{1t} = -\frac{0.5200}{(0.0584)} + \frac{1.1536}{(0.0000)} \hat{\Delta}_{1(t-1)} + \hat{\varepsilon}_t \quad (24)$$

The STE is  $-0.52$  and is only significant at the 10 % level.

In the second estimation, Brazil is excluded from the donor pool. Appendix Table 9 and Fig. 8 show the result of this setting. Here again, the Engle-Granger test indicates the presence of a cointegration relationship at the 5 % significance level. Regarding the post-Brexit referendum period, the behaviours of the actual and predicted curves are similar to those of the first estimate including the break in 2017Q4. However, it is remarkable that between 2016Q3-2017Q4 the prediction fits very closely the actual path and its turning points. Again, the ATE, which is 2.00 billion British pounds, is not significantly different from zero. The treatment effects are again serially correlated and fitted by a (non-stationary) AR(1) model:

$$\hat{\Delta}_{1t} = -\frac{0.4448}{(0.0936)} + \frac{1.0760}{(0.0000)} \hat{\Delta}_{1(t-1)} + \hat{\varepsilon}_t \quad (25)$$

The STE in the second estimation is  $-0.44$  but narrowly significant at the 10 % level. Since the impact of the Brexit process on the GFCF becomes apparent in 2018, the low ATE and STE significances in both estimates are not surprising results.<sup>12</sup>

Because of that, a third estimate is performed, where the cut-off point  $T_1$  is set to 2017Q4. The summarized results can be seen in Appendix Table 10, whereas the actual and counterfactual predicted values are plotted in Fig. 9. Additionally to the predictors in the second estimate, the LASSO-LOO procedure also picked Korea as predictor. Again, the  $p$  value of the Engle-Granger test (0.0098) indicates a close cointegration relationship. Particularly between 2016Q1 and 2017Q4 the prediction closely matches the actual data including its turning points. The ATE in the third estimate is  $-2.92$  billion British pounds and is significant at the 1 % level.<sup>13</sup> The sum of the treatment effects reveals that the cumulative treatment effect between 2018Q1 and 2019Q2 is approximately  $-17.5$  billion British Pounds.

#### 4.4 Results for exports

Appendix Tables 11 and 12 display the summarized results of the estimates for the export panel data, whereas Figs. 10 and 11 illustrate the actual and predicted values for exports. At first glance, the positive treatment effect stands out, where a strong drop of the actual data can be seen at the end in 2019Q2. All in all, the actual path appears to be more volatile after the Brexit vote than during the period before. In Fig. 12, the UK's exports and the British pound / US dollar exchange rate are plotted.<sup>14</sup> The (lagged) parallelism of both series is remarkable. Apparently, a reason for the increasing export activity in the post-Brexit vote period could be the depreciation of the British pound, as a consequence of the Brexit process, which made UK goods more competitive.<sup>15</sup> This positive impulse on exports appears to be a short-term phenomenon, since it loses momentum about 5 quarters after the Brexit referendum.

Using the complete export panel data, the LASSO-LOO procedure picks Canada, United States and Brazil as predictors of the counterfactual. The Engle-Granger test of this first estimate implies that the null hypothesis of no cointegration can be rejected with the  $p$  value of 0.060. Using the BIC, a

<sup>12</sup> The delayed impact of the Brexit process on investment could be explained by the changed expectations for soft and hard Brexit after the EU-UK negotiations started in the second half of 2017. Another reason could be the reorganisation of production, particularly in supply chains, where planning and implementation may show some delay.

<sup>13</sup> Since in these settings only six observations for the treatment effects are present, the use of an AR-model is limited. Hence, only the ATE using Newey-West standard errors is calculated in order to deal with the serial correlation.

<sup>14</sup> Monthly exchange rate data are extracted from the Monthly Monetary and Financial Statistics of the OECD database and recalculated to compile quarterly data by taking the mean of three months.

<sup>15</sup> The impact of Brexit on British pound exchange rates has been investigated by Korus and Celebi (2019). They find that particularly the Brexit vote and “bad”/“hard” Brexit news have led to a depreciation of the British pound exchange rate against both the US dollar and the euro.

constant model fits the treatment effects the best, so that an AR-model is not required. The ATE of the Brexit process on exports is 4.81 billion British pounds and, according to the HAC t-statistic, is statistically significant at the 1 % level. In the first estimate, the cumulative treatment effect is 57.7 billion British pounds.

In the second estimate, Brazil is excluded from the donor pool, so that the LASSO-LOO procedure picked Australia, Canada, Israel, Japan, Korea, New Zealand, Turkey and the United States as predictors. The Engle-Granger p value drops slightly to 0.058. In this broader predictor constellation, the ATE increases to 9.01 and is again statistically significant at the 1 % level. In this set-up, the BIC approach leads to an AR(1) fitting:

$$\hat{\Delta}_{1t} = \underbrace{9.8315}_{(0.0000)} + \underbrace{0.0285}_{(0.8929)} \hat{\Delta}_{1(t-1)} + \hat{\varepsilon}_t \quad (26)$$

The STE is 9.83 billion British pounds and is significantly different from zero at the 1 % level. Since the dynamics of the AR-model are rather low, LTE is close to STE but not significant, which supports also the short-term phenomenon conjecture. In the second estimate, the cumulative treatment effect is 108.1 billion British pounds.

## 5 Conclusion

In this paper, the impact of the Brexit process on the British real economy is investigated. In technical terms, this study shows the adequacy of the PDA of Hsiao et al. (2012) to quantify the treatment effects in the case of the Brexit. Comparing it with the topically related article of Born et al. (2019), where the SCM is adopted to analyse the impact of Brexit, the PDA stands out in two different ways. Firstly, in contrast to the SCM, the use of the PDA allows to conduct inference. Secondly, the PDA is on the whole more flexible and thus can be used for a wider range of macroeconomic variables due to the simplicity of the computation. In the case of Brexit, the method can still be performed even in the absence of European Single Market member countries.

Taken as a whole, the results indicate that although the Brexit was not yet officially a *fait accompli*, the whole process has already had an impact on the real economy of the UK. Apparently, the upcoming Brexit and thus changing economic framework conditions had – at least to some extent – already been anticipated before the UK withdrew from the EU on 31 January 2020. Note that, despite the calculated LTE, the used technique cannot predict the future, since the executed Brexit could lead to a structural break.

All measures for the impact of the Brexit process on real GDP growth are negative and significantly different from zero at any significance level. Thus, there is very strong evidence that the Brexit process has already cost the UK in terms of economic growth. The results show that the ATE of the Brexit process on real GDP growth is between –1.0 and –1.4 percentage points. Taking into account that the first estimate is likely affected by a country-specific shock in

Turkey, the ATE ranges most likely between  $-1.3$  and  $-1.4$  percentage points approximately. Due to autoregressive dynamics, the LTE ranges between approximately  $-1.39$  and  $-1.46$  percentage points and is again highly significant.

The ATE on British GDP, in terms of 2016 British pounds, ranges between  $-4.0$  and  $-4.5$  billion but narrowly misses the 10 % significance level. The STE is  $-1.36$  for both conducted estimates and again is highly significant. The calculated LTE in both estimates are quite dispersed, namely  $-39$  and  $-117$  billion British pounds. Although the report of an accurate level for the LTE is therefore difficult, both estimated figures are again highly significant. However, the figures for the cumulative loss of the Brexit process since the vote in both estimates are relatively close, namely 48 and 54 billion British pounds. The gap between the actual and counterfactual GDP ranges between 2.5 and 2.7%.

To compare these results with the findings of Born et al. (2019), the estimated figures have to be adjusted, since the sample of Born et al. (2019) ends in 2018Q4. Additionally, since a number of countries revised their GDP calculations due to methodological improvements in 2019Q2, the comparison should be treated with caution.<sup>16</sup> By the end of 2018, the gap between the actual and counterfactual prediction estimated with the PDA ranges between 1.3 and 1.7%, whereas Born et al. (2019) predict, generally speaking, a higher gap, namely 1.7 to 2.4%. The cumulative loss of both estimates conducted with the PDA is approximately 25 and 29 billion British pounds by the end of 2018, whereas Born et al. (2019) estimate 55 billion British pounds regarding the counterfactual with a 2.4% gap.

A proper comparison of results stemming from the SCM and PDA could be made using the estimates of Springford (2019) who, broadly speaking, replicates the SCM approach of Born et al. (2019) using updated (revised) data.<sup>17</sup> The calculated gap between the actual and counterfactual GDP here is 2.9% and is, therefore, about 0.2 to 0.4 percentage points higher than the estimated figures using the PDA.

Both Born et al. (2019, p. 2735) and Springford (2019) generate counterfactual projections for the UK's consumption, GFCF, imports and exports by simply decomposing the response of the UK's GDP into its components. Thus, these projections are predictions of the GDP counterfactual prediction. That is why this technique can only point out the direction of the impact of the Brexit process. By contrast, the PDA approach is able to construct counterfactual predictions directly.

Using the PDA on the private consumption panel data, the results show that the estimated ATE on the UK's private consumption is  $-4.7$  billion British pounds and is significant at the 5 % level. The cumulative treatment effect since the Brexit vote is  $-56$  billion British pounds.

<sup>16</sup> See, for example, the Office for National Statistics (2019), section 7 ("Revision to GDP").

<sup>17</sup> Note that Springford (2019) also uses European Single Market member countries in the donor pool, which could bias the estimated figures as in Born et al. (2019).

The results for the GFCF panel show that there is no impact of the Brexit process on the UK's fixed investments until the end of 2017. From 2018Q1 on, the actual and predicted fixed investments diverge with an ATE of  $-2.9$  billion British pounds, which is significant at the 1 % level. Starting from 2018Q1, the resulting cumulative treatment effect is  $-17.5$  billion British pounds.

The PDA results for British exports illustrate a positive impact of the Brexit process. The ATE is 4.8 billion British pounds and significantly different from zero at the 1 % level, whereas the cumulative treatment effect is approximately 58 billion British pounds. These results are contrary to the projection of Springford (2019), who estimates lower actual exports than predicted. Regarding the UK's exports path and the British pound / US dollar exchange rate, the positive impact could be due to the depreciation of the British currency, which increased the competitiveness of the UK. Note that the positive impact on exports appears to be a short-term impulse.

### 5.1 Further perspectives and policy conclusions

Regarding these results, it is advisable for the EU and, more importantly, the UK to abandon the 'game of chicken' as soon as possible in order to finalise a Brexit deal by which the UK retains at least a certain degree of access to the European Single Market. Although households have anticipated the upcoming Brexit to a certain extent, it is uncertain whether a no deal Brexit in the end of 2020 will cause a further structural break and further negative impulses.

To redeem the losses incurred through Brexit, the British government has two key policy elements available. Firstly, the government can seek to boost growth via expansive fiscal policies. Especially in the current phase, where private consumption and investment in the UK are declining due to Brexit and interest rates are relatively low, the possibility of a crowding out effect is lower than usual. In addition to that, the UK's long-term government bond yields are at historically low rates, which favour the funding of fiscal expenditures.

Possible policies could be tax reductions - above all in relation to personal income taxes and corporate taxes - which could particularly stimulate the economic activity through higher work and production incentives (Devereux and Love 1994). In addition to that, a reform of capital income taxes could notably foster growth via two channels: firstly, this policy could increase private investments (Rebelo 1991). Combined with well-targeted tax incentives, in particular for research and development (R&D) investments, lower capital income taxation could increase the productivity of the UK (IMF 2015). Secondly, in line with Froot and Stein (1991), the devaluation of the British pound attracts foreign investment, which foster economic growth. Combined with reforms for easing business procedures and providing access for foreign investors to the domestic credit market, a declining tax rate on capital income would boost in particular foreign direct investment (FDI).

Related to this issue, an expansive monetary policy could also help to stimulate growth due to increasing consumption and investment incentives. Moreover, the expansive monetary policy could lead to a further

depreciation of the pound sterling, which would increase exports and foreign investments.

Further possible policies could be public infrastructure and R&D investments. In particular, higher education and health investments could be helpful to attract human capital, which is known as a main driver of long-term growth (Lucas 1988) (Barro 2001). Since technological progress and intangible assets are also main drivers of growth, the enlargement of R&D investments, which include also positive externalities, should be prioritised (Demmou et al. 2019). At this point, the British government can realise this through tax breaks or subsidy incentives or by directly investing in R&D.

The second key element to redeem the losses of Brexit is the concluding of free trade agreements. Because of the strong economic ties between the UK and the US, an adapted version of the Transatlantic Trade and Investment Partnership (TTIP) agreement could foster the growth of the UK's economy the most. Estimated growth gains stemming from the TTIP do not yet exist for the UK. However, Jungmittag and Welfens (2016) estimated for Germany a real income gain of 2%. Assuming that this estimated figure would also be an appropriate prediction for the possible gain of the UK due to the adapted TTIP, a large proportion of the current estimated gap between the actual and counterfactual prediction could be compensated via such an agreement. However, it must be remembered that such trade agreements are not usually realised in the short-run. Therefore, the discussed fiscal policy measures stand out as the primary key element to offset the losses of the Brexit.

Based on the econometric method used here, future research dealing with the impact of the Brexit process on the UK's FDI inflows and the UK's domestic value-added in gross exports could reveal some further information about the external trade changes. A very interesting issue in future will be the effects of the Brexit day itself, now most likely to be January 31, 2020. Several quarters after the official completion of the Brexit process, the econometric method presented in this paper can be repeated in order to measure the treatment effects for the, by then, non-EU member UK. Additionally, further investigations dealing with the impact of Brexit could be interesting, in which causal implications among macroeconomic variables such as GDP, consumption and GFCF are explored.

## Appendix

**Table 2** Counterfactual prediction of the UK's real GDP growth rates in percent using all donors (first estimation)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	2.5623	0.9249	2.7705
Australia	-0.5099	0.1731	-2.9464
Brazil	-0.0394	0.0616	-0.6398
Canada	0.0176	0.1771	0.0993
China	-0.3798	0.1532	-2.4797
India	0.1449	0.0759	1.9077
Israel	-0.1682	0.1794	-0.9374
Japan	-0.0602	0.0606	-0.9936
Korea	0.1859	0.1305	1.4247
Mexico	-0.2525	0.0938	-2.6925
New Zealand	0.3948	0.1147	3.4429
Russia	0.2805	0.0419	6.6862
Turkey	0.1355	0.0320	4.2279
United States	0.5684	0.1142	4.9771

$R^2 = 0.9830$

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	1.91	1.92	-0.01
2016 Q4	1.81	2.09	-0.28
2017 Q1	2.23	2.53	-0.31
2017 Q2	1.94	2.75	-0.81
2017 Q3	1.83	3.75	-1.92
2017 Q4	1.58	3.31	-1.73
2018 Q1	1.05	3.10	-2.05
2018 Q2	1.33	3.34	-2.01
2018 Q3	1.62	2.58	-0.96
2018 Q4	1.54	2.39	-0.86
2019 Q1	2.07	2.25	-0.19
2019 Q2	1.31	2.12	-0.82
Mean	1.68	2.68	-0.99
Std. dev.	0.34	0.58	0.75
<i>T</i>	4.90	4.62	-1.32

Constant OLS model with HAC standard errors:

ATE = -0.9950      Std.dev. = 0.3081       $T = -3.2298$       p value = 0.0080

Treatment fits to a stationary AR(4)-model:

LTE = -1.2226 (Wald-stat. = 9.9648)

**Table 3** Counterfactual prediction of the UK's real GDP growth rates in percent after removing Turkey from the donor pool (second estimation)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	2.0447	1.2311	1.6608
Australia	-0.6017	0.2306	-2.6095
Brazil	-0.0870	0.0814	-1.0696
Canada	-0.0012	0.2377	-0.0049
China	-0.2912	0.2038	-1.4291
India	0.1534	0.1020	1.5046
Israel	0.0842	0.2272	0.3706
Japan	0.0453	0.0742	0.6113
Korea	0.0825	0.1721	0.4790
Mexico	-0.1897	0.1244	-1.5254
New Zealand	0.3764	0.1539	2.4459
Russia	0.2872	0.0563	5.1017
United States	0.6292	0.1521	4.1353

R<sup>2</sup> = 0.9679

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	1.91	3.10	-1.20
2016 Q4	1.81	2.81	-1.00
2017 Q1	2.23	2.82	-0.59
2017 Q2	1.94	2.85	-0.91
2017 Q3	1.83	2.94	-1.11
2017 Q4	1.58	3.12	-1.54
2018 Q1	1.05	3.15	-2.10
2018 Q2	1.33	3.42	-2.09
2018 Q3	1.62	2.99	-1.37
2018 Q4	1.54	3.35	-1.82
2019 Q1	2.07	3.36	-1.29
2019 Q2	1.31	2.93	-1.62
Mean	1.68	3.07	-1.39
Std. dev.	0.34	0.22	0.47
<i>T</i>	4.90	14.16	-2.98

Constant OLS model with HAC standard errors:

ATE = -1.3874      Std.dev. = 0.1895      *T* = -7.3196      p value = 0.0000

Treatment fits to a stationary AR(1)-model:

LTE = -1.4604 (Wald-stat. = 7.4559)

**Table 4** Counterfactual prediction of the UK's real GDP growth rates in percent after removing Turkey, Brazil, India and Mexico from the donor pool (third estimation)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)			
	Coefficient	Std.dev.	<i>T</i>
Constant	3.4726	1.1396	3.0472
Australia	-0.5050	0.2080	-2.4276
Canada	-0.3483	0.1517	-2.2964
China	-0.4919	0.1423	-3.4561
Israel	0.3536	0.1610	2.1965
Japan	0.0047	0.0727	0.0641
Korea	0.1894	0.1324	1.4306
New Zealand	0.2710	0.1300	2.0837
Russia	0.2173	0.0510	4.2573
United States	0.7043	0.1593	4.4224
$R^2 = 0.9577$			
Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)			
	Actual	Predicted	Treatment
2016 Q3	1.91	3.01	-1.10
2016 Q4	1.81	2.94	-1.13
2017 Q1	2.23	2.93	-0.71
2017 Q2	1.94	2.32	-0.38
2017 Q3	1.83	2.59	-0.76
2017 Q4	1.58	2.78	-1.21
2018 Q1	1.05	3.28	-2.23
2018 Q2	1.33	3.40	-2.06
2018 Q3	1.62	3.08	-1.46
2018 Q4	1.54	3.43	-1.90
2019 Q1	2.07	3.22	-1.15
2019 Q2	1.31	2.92	-1.61
Mean	1.68	2.99	-1.31
Std. dev.	0.34	0.33	0.57
<i>T</i>	4.90	9.18	-2.31
Constant OLS model with HAC standard errors:			
ATE=-1.3078	Std.dev. = 0.2248	<i>T</i> = -5.8165	p value=0.0001

Treatment fits to a stationary AR(1)-model:

LTE = -1.3871 (Wald-stat. = 8.8885)

**Table 5** Counterfactual prediction of the UK’s GDP (in billion British pounds, CVM) (first estimate)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	-51.7130	20.0640	-2.5774
Japan	0.0008	0.0003	3.0466
Korea	-0.0003	0.0001	-5.5885
United States	0.1277	0.0097	13.1580

R<sup>2</sup> = 0.9838

Engle-Granger cointegration tau-statistic = -4.28 (p value = 0.06824)

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	499.84	497.96	1.87
2016 Q4	503.08	500.06	3.02
2017 Q1	505.98	503.34	2.64
2017 Q2	507.26	506.17	1.08
2017 Q3	508.98	509.65	-0.67
2017 Q4	511.01	515.16	-4.14
2018 Q1	511.30	517.15	-5.85
2018 Q2	514.02	522.07	-8.05
2018 Q3	517.22	525.15	-7.93
2018 Q4	518.87	525.87	-7.00
2019 Q1	521.87	531.61	-9.74
2019 Q2	520.74	533.85	-13.11
Mean	511.68	515.67	-3.99
Std. dev.	7.06	12.28	5.44
<i>T</i>	72.50	42.01	-0.73

Constant OLS model with HAC standard errors:

ATE = -3.9898	Std.dev. = 2.3928	<i>T</i> = -1.6674	p value = 0.12362
---------------	-------------------	--------------------	-------------------

Treatment fits to a stationary AR (2)-model:

LTE = -39.036 (Wald-stat. = 85.4672)

**Table 6** Counterfactual prediction of the UK's GDP (in billion British pounds, CVM) after removing Japan from the donor pool (second estimate)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)			
	Coefficient	Std.dev.	<i>T</i>
Constant	-9.0572	18.5240	-0.4889
Australia	-0.2821	0.1319	-2.1394
Canada	0.1017	0.1142	0.8900
Korea	-0.0001	0.0001	-1.3959
United States	0.1457	0.0119	12.2590
$R^2 = 0.9820$			
Engle-Granger cointegration tau-statistic=-4.52 (p value=0.0898)			
Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)			
	Actual	Predicted	Treatment
2016 Q3	499.84	498.27	1.57
2016 Q4	503.08	500.06	3.02
2017 Q1	505.98	503.26	2.72
2017 Q2	507.26	506.21	1.05
2017 Q3	508.98	509.36	-0.37
2017 Q4	511.01	514.83	-3.82
2018 Q1	511.30	517.49	-6.19
2018 Q2	514.02	522.18	-8.17
2018 Q3	517.22	526.69	-9.47
2018 Q4	518.87	527.84	-8.97
2019 Q1	521.87	532.74	-10.87
2019 Q2	520.74	535.12	-14.39
Mean	511.68	516.17	-4.49
Std. dev.	7.06	12.84	5.98
<i>T</i>	72.50	40.21	-0.75
Constant OLS model with HAC standard errors:			
ATE=-4.4897	Std.dev. = 2.6641	<i>T</i> = -1.6853	p value=0.1200

Treatment fits to a stationary AR (2)-model:

LTE = -117.104 (Wald-stat. = 153.587)

**Table 7** Counterfactual prediction of the UK’s private consumption (in billion British pounds, CVM)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	-20.8660	27.9190	-0.7474
Australia	-0.9172	0.0955	-9.6040
Japan	0.0014	0.0003	4.1043
New Zealand	3.6082	1.2760	2.8278
United States	0.1121	0.0153	7.3239

R<sup>2</sup> = 0.9848

Engle-Granger cointegration tau-statistic = -5.04 (p value = 0.0346)

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	327,260	325,933.61	1326.39
2016 Q4	328,703	327,746.04	956.96
2017 Q1	330,363	331,143.53	-780.53
2017 Q2	331,307	333,731.63	-2424.63
2017 Q3	332,521	334,573.24	-2052.24
2017 Q4	333,573	338,078.90	-4505.90
2018 Q1	335,383	338,811.42	-3428.42
2018 Q2	337,034	342,269.35	-5235.35
2018 Q3	337,889	345,938.28	-8049.28
2018 Q4	338,478	347,928.02	-9450.02
2019 Q1	339,451	348,883.64	-9432.64
2019 Q2	340,488	353,403.38	-12,915.38
Mean	334,370.83	339,036.75	-4665.92
Std. dev.	4398.22	8795.70	4487.02
<i>T</i>	76.02	38.55	-1.04

Constant OLS model with HAC standard errors:

ATE = -4.6659	Std.dev. = 1.9285	<i>T</i> = -2.4194	p value = 0.0340
---------------	-------------------	--------------------	------------------

Treatment fits to a non-stationary AR (2)-model

**Table 8** Counterfactual prediction of the UK's GFCF (in billion British pounds, CVM) (first estimate)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	33.2430	7.3437	4.5267
Australia	-0.3980	0.0811	-4.9052
Brazil	0.1121	0.0666	1.6843
Japan	0.0005	0.0004	1.2599
New Zealand	-0.1004	0.8921	-0.1125
United States	0.0813	0.0233	3.4877

 $R^2 = 0.9449$ 

Engle-Granger cointegration tau-statistic=-6.23 (p value=0.0076)

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	86.82	85.74	1.07
2016 Q4	86.30	84.90	1.41
2017 Q1	86.34	86.05	0.29
2017 Q2	87.55	86.38	1.17
2017 Q3	87.22	85.39	1.83
2017 Q4	88.20	87.25	0.95
2018 Q1	87.36	87.57	-0.21
2018 Q2	86.98	88.63	-1.65
2018 Q3	87.40	88.69	-1.29
2018 Q4	87.31	89.85	-2.54
2019 Q1	88.07	91.06	-2.99
2019 Q2	87.24	92.18	-4.94
Mean	87.23	87.81	-0.57
Std. dev.	0.58	2.32	2.11
<i>T</i>	150.44	37.77	-0.27

Constant OLS model with HAC standard errors:

ATE=-0.5748	Std.dev. = 0.8953	<i>T</i> = -0.6421	p value=0.5340
-------------	-------------------	--------------------	----------------

Treatment fits to a non-stationary AR (1)-model

**Table 9** Counterfactual prediction of the UK’s GFCF (in billion British pounds, CVM) after removing Brazil from the donor pool (second estimate)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	32.7780	7.5674	4.3315
Australia	-0.2867	0.0485	-5.9072
Japan	0.0005	0.0004	1.3520
New Zealand	0.0296	0.9165	0.0323
United States	0.0720	0.0234	3.0830

R<sup>2</sup> = 0.9393

Engle-Granger cointegration tau-statistic = -5.39 (p value = 0.0173)

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	86.82	86.10	0.72
2016 Q4	86.30	85.66	0.64
2017 Q1	86.34	86.72	-0.38
2017 Q2	87.55	87.20	0.35
2017 Q3	87.22	86.53	0.69
2017 Q4	88.20	88.06	0.14
2018 Q1	87.36	88.43	-1.06
2018 Q2	86.98	89.49	-2.51
2018 Q3	87.40	89.17	-1.78
2018 Q4	87.31	90.29	-2.98
2019 Q1	88.07	91.41	-3.34
2019 Q2	87.24	92.13	-4.89
Mean	87.23	88.43	-1.20
Std. dev.	0.58	2.11	1.88
<i>T</i>	150.44	41.88	-0.64

Constant OLS model with HAC standard errors:

ATE = -1.1995      Std.dev. = 0.7966      *T* = -1.5059      p value = 0.1603

Treatment fits to a non-stationary AR(1)-model

**Table 10** Counterfactual prediction of the UK's GFCF (in billion British pounds, CVM) after removing Brazil from the donor pool and with cut-off point 2018Q1 (third estimate)

Panel A: Weights of LASSO-predictors for the period 2008Q1 – 2017Q4

	Coefficient	Std.dev.	<i>T</i>
Constant	28.5660	8.9588	3.1886
Australia	-0.2834	0.0419	-6.7580
Japan	0.0007	0.0004	1.6845
Korea	3.68E-05	4.30E-05	0.8562
New Zealand	-0.1624	0.9055	-0.1794
United States	0.0689	0.0206	3.3429

 $R^2 = 0.9640$ 

Engle-Granger cointegration tau-statistic=-5.93 (p value=0.0098)

Panel B: Treatment effects in the period 2018Q4 – 2019Q2

	Actual	Predicted	Treatment
2018 Q1	87.36	88.90	-1.54
2018 Q2	86.98	89.82	-2.83
2018 Q3	87.40	89.20	-1.81
2018 Q4	87.31	90.45	-3.14
2019 Q1	88.07	91.33	-3.25
2019 Q2	87.24	92.20	-4.96
Mean	87.23	88.73	-2.92
Std. dev.	0.58	1.98	1.22
<i>T</i>	150.44	44.92	-2.39

Constant OLS model with HAC standard errors:

ATE=-2.9226      Std.dev. = 0.5628       $T = -5.1929$       p value=0.0035

Treatment fits to a non-stationary AR(2)-model

**Table 11** Counterfactual prediction of the UK's exports (in billion British pounds, CVM) (first estimation)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)

	Coefficient	Std.dev.	<i>T</i>
Constant	34.9180	6.2522	5.5850
Brazil	0.8180	0.3679	2.2238
Canada	0.2656	0.0818	3.2459
United States	0.0520	0.0215	2.4161

 $R^2 = 0.9177$ 

Engle-Granger cointegration tau-statistic = -4.34 (p value = 0.0604)

Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)

	Actual	Predicted	Treatment
2016 Q3	138.54	138.83	-0.29
2016 Q4	147.01	138.63	8.38
2017 Q1	147.66	141.04	6.61
2017 Q2	151.19	143.05	8.14
2017 Q3	152.77	142.53	10.24
2017 Q4	150.51	142.99	7.52
2018 Q1	149.44	144.19	5.25
2018 Q2	145.60	145.33	0.27
2018 Q3	150.59	146.32	4.27
2018 Q4	151.30	147.66	3.64
2019 Q1	153.66	146.60	7.06
2019 Q2	143.54	146.94	-3.40
Mean	148.48	143.68	4.81
Std. dev.	4.31	3.06	4.10
<i>T</i>	34.46	46.95	1.17

Constant OLS model with HAC standard errors:

ATE = 4.80732	Std.dev. = 1.2688	<i>T</i> = 3.78899	p value = 0.0030
---------------	-------------------	--------------------	------------------

**Table 12** Counterfactual prediction of the UK's exports (in billion British pounds, CVM) after removing Brazil from the donor pool (second estimate)

Panel A: Weights of LASSO-predictors for the pre-Brexit referendum period (2008Q1 – 2016Q2)			
	Coefficient	Std.dev.	<i>T</i>
Constant	15.6880	12.7280	1.2325
Australia	-0.4881	0.1786	-2.7322
Canada	0.7291	0.1296	5.6260
Israel	0.1428	0.1693	0.8433
Japan	-0.0001	0.0006	-0.2385
Korea	0.0003	0.0001	3.3446
New Zealand	3.6418	1.1355	3.2071
Turkey	-0.3170	0.1214	-2.6117
United States	-0.0877	0.0551	-1.5925
$R^2 = 0.9594$			
Engle-Granger cointegration tau-statistic = -6.18 (p value = 0.05820)			
Panel B: Treatment effects in the post-Brexit referendum period (2016Q3 – 2019Q2)			
	Actual	Predicted	Treatment
2016 Q3	138.54	141.62	-3.07
2016 Q4	147.01	137.45	9.56
2017 Q1	147.66	138.47	9.18
2017 Q2	151.19	139.04	12.15
2017 Q3	152.77	138.32	14.45
2017 Q4	150.51	136.02	14.48
2018 Q1	149.44	136.83	12.61
2018 Q2	145.60	139.75	5.85
2018 Q3	150.59	141.60	8.99
2018 Q4	151.30	141.38	9.91
2019 Q1	153.66	140.27	13.39
2019 Q2	143.54	142.92	0.62
Mean	148.48	139.47	9.01
Std. dev.	4.31	2.15	5.47
<i>T</i>	34.46	64.87	1.65
Constant OLS model with HAC standard errors:			
ATE=9.0109	Std.dev. = 1.6450	<i>T</i> = 5.4776	p value = 0.0002

**Table 13** Descriptive statistics for the whole sample and for the pre- and post-Brexit referendum period

Panel A: real GDP in % (year-on-year)															
Period	AUSTRALIA	BRAZIL	CANADA	CHINA	INDIA	ISRAEL	JAPAN	KOREA	MEXICO	NEW ZEALAND	RUSSIA	TURKEY	UNITED KINGDOM	UNITED STATES	
<b>2008q1-2019q2</b>	Mean	2.57	1.54	8.03	7.07	3.49	0.57	3.10	1.99	2.20	1.28	4.62	1.19	1.67	
	Median	2.55	1.24	1.82	7.45	7.04	0.70	2.92	2.75	2.67	1.64	5.33	1.86	2.07	
	Maximum	4.72	9.04	3.80	12.20	13.69	5.78	5.51	7.78	7.27	4.78	11.00	2.82	3.98	
	Minimum	1.40	-5.47	-4.02	6.20	0.16	-0.15	-8.68	-1.91	-7.76	-2.33	-9.40	-12.53	-5.81	-3.92
	Std. Dev.	0.68	3.49	1.77	1.67	2.20	1.44	2.57	1.87	2.66	1.66	3.81	5.02	2.04	1.74
<b>2008q1-2016q2</b>	Mean	2.63	1.93	1.45	8.53	7.07	0.34	3.25	2.01	1.91	1.18	5.02	1.01	1.38	
	Median	2.60	2.57	1.78	7.90	6.98	3.56	3.24	2.86	2.25	1.69	5.84	1.98	1.72	
	Maximum	4.72	9.04	3.65	12.20	13.69	5.78	5.51	7.78	7.27	4.78	11.00	2.82	3.98	
	Minimum	1.40	-5.47	-4.02	6.40	0.16	-0.15	-8.68	-1.91	-7.76	-2.33	-9.40	-12.53	-5.81	-3.92
	Std. Dev.	0.73	3.92	1.99	1.68	2.50	1.64	2.94	2.13	3.05	1.82	4.42	5.22	2.35	1.93
<b>2016q3-2019q2</b>	Mean	2.41	0.45	2.13	6.63	7.06	3.73	1.21	1.94	3.01	1.56	3.50	1.68	2.48	
	Median	2.41	0.93	1.88	6.70	7.09	3.58	1.28	1.88	3.06	1.64	4.70	1.71	2.47	
	Maximum	3.12	2.23	3.80	6.80	8.59	4.75	2.36	3.77	3.28	4.07	11.02	2.23	3.20	
	Minimum	1.44	-2.50	1.30	6.20	5.11	2.95	0.17	1.60	0.10	2.12	0.48	1.05	1.56	
	Std. Dev.	0.53	1.43	0.75	0.20	0.98	0.63	0.70	0.59	1.04	0.53	0.77	4.43	0.34	0.48
Panel B: real GDP, chained volume measures; seasonally adjusted; all figures in million local currencies															
Period	AUSTRALIA	BRAZIL	CANADA	INDIA	ISRAEL	JAPAN	KOREA	MEXICO	NEW ZEALAND	RUSSIA	TURKEY	UNITED KINGDOM	UNITED STATES		
<b>2008q1-2019q2</b>	Mean	415,094	290,292	469,431	25,478	277,186	127,030,260	393,591,967	4,125,655	53,998	21,269,543	474,236	4,199,644		
	Median	415,004	293,668	471,236	24,527	277,173	126,980,238	394,389,000	4,089,546	52,603	21,542,643	469,497	4,143,528		
	Maximum	475,208	311,519	523,082	36,225	333,287	134,764,125	459,813,400	4,648,487	63,427	22,482,099	441,754	4,755,465		
	Minimum	360,869	253,376	418,835	17,051	229,480	115,824,900	324,843,200	3,470,290	47,374	19,040,657	242,931	3,783,529		
	Std. Dev.	35,945	15,366	30,696	5910	32,644	4,692,301	41,122,204	356,614	5114	951,423	64,545	28,183	294,165	
<b>2008q1-2016q2</b>	Mean	398,850	289,147	455,694	22,654	262,251	125,009,390	375,364,218	3,964,669	51,511	20,988,128	461,021	4,060,596		

Table 13 (continued)

Median	401,001	293,668	455,882	22,372	261,651	125,184,013	376,676,800	3,976,907	50,884	21,389,780	310,984	458,676	4,041,028
Maximum	443,841	311,519	487,481	30,030	301,407	129,720,100	425,793,300	4,406,333	58,498	22,274,887	395,713	497,593	4,409,854
Minimum	360,869	253,376	418,835	17,051	229,480	115,824,900	324,843,200	3,470,290	47,374	19,040,657	242,931	433,618	3,783,529
Std. Dev.	26,181	17,663	22,438	3852	23,239	3,637,374	30,952,929	263,736	3235	938,868	49,015	19,409	193,774
<b>2016q3-2019q2</b>													
Mean	461,117	293,536	508,353	33,479	319,501	132,756,058	445,237,258	4,581,783	61,044	22,066,886	424,396	511,681	4,593,613
Median	462,166	294,254	509,776	33,593	320,691	133,107,588	445,986,850	4,604,952	61,018	22,115,596	428,792	511,157	4,595,090
Maximum	475,208	298,399	523,082	36,225	333,287	134,764,125	459,813,400	4,648,487	63,427	22,482,099	441,754	521,873	4,755,465
Minimum	444,489	286,315	490,086	30,523	305,027	130,061,025	427,931,900	4,456,441	58,810	21,523,775	383,560	499,836	4,433,769
Std. Dev.	10,144	3811	10,409	1970	9815	1,411,626	10,341,776	67,186	1522	346,937	17,159	7057	110,782
Panel C: real private consumption, all figures in million local currencies													
<b>Period</b>	<b>AUSTRALIA</b>	<b>BRAZIL</b>	<b>CANADA</b>	<b>INDIA</b>	<b>ISRAEL</b>	<b>JAPAN</b>	<b>KOREA</b>	<b>MEXICO</b>	<b>NEW ZEALAND</b>	<b>RUSSIA</b>	<b>TURKEY</b>	<b>UNITED KINGDOM</b>	<b>UNITED STATES</b>
<b>2008q1-2019q2</b>													
Mean	231,491	191,229	265,867	14,300	150,818	73,144,982	195,028,074	2,758,240	32,466	11,502,168	211,963	305,220	2,879,983
Median	231,211	194,801	264,675	13,906	147,695	73,547,125	194,740,000	2,714,679	31,731	11,588,636	218,152	299,613	2,803,884
Maximum	263,544	209,618	301,766	20,439	186,191	76,513,400	221,901,200	3,118,079	39,273	13,332,278	269,154	340,488	3,312,510
Minimum	200,484	160,679	234,310	9339	122,972	69,200,450	167,793,600	2,375,293	27,463	9,742,847	151,584	279,557	2,604,334
Std. Dev.	19,757	13,591	21,370	3419	19,982	1,802,476	15,216,652	221,146	3698	897,220	36,406	20,579	221,958
Mean	222,638	189,107	255,898	12,664	141,290	72,580,298	188,019,665	2,650,891	30,625	11,368,413	196,810	294,932	2,771,053
Median	224,866	193,140	254,856	12,612	140,292	72,903,300	188,309,700	2,647,181	30,350	11,390,793	195,359	291,572	2,745,361
Maximum	246,742	209,618	280,644	16,608	168,741	76,513,400	205,868,800	2,904,474	35,292	13,332,278	244,431	323,666	3,052,821
Minimum	200,484	160,679	234,310	9339	122,972	69,200,450	167,793,600	2,375,293	27,463	9,742,847	151,584	279,557	2,604,334
Std. Dev.	14,598	15,166	14,730	2216	13,227	1,757,780	10,639,067	141,873	2192	999,594	29,551	12,369	134,926
Mean	256,576	197,244	294,112	18,934	177,815	74,744,921	214,885,233	3,062,396	37,685	11,881,142	254,897	334,371	3,188,619
Median	257,382	198,061	295,599	18,852	178,124	74,843,763	215,620,600	3,080,371	37,709	11,925,051	255,590	334,478	3,189,077
Maximum	263,544	201,701	301,766	20,439	186,191	75,580,775	221,901,200	3,118,079	39,273	12,318,613	269,154	340,488	3,312,510
Minimum	248,095	191,820	282,775	17,209	170,330	73,928,925	207,332,600	2,953,279	35,818	11,399,315	237,246	327,260	3,072,266

**Table 13** (continued)

	Std. Dev.	5365	3488	6307	1171	5735	493,518	5,069,021	56,078	1152	289,233	9034	4398	79,578
Panel D: real gross fixed capital formation, all figures in million local currencies														
<b>Period</b>		AUSTRALIA	BRAZIL	CANADA	INDIA	ISRAEL	JAPAN	KOREA	MEXICO	NEW ZEALAND	RUSSIA	TURKEY	UNITED KINGDOM	UNITED STATES
<b>2008q1-2019q2</b>	Mean	106,269	58,329	107,116	8247	55,208	29,374,886	116,530,515	878,797	12,323	4,684,755	96,043	78,812	837,957
	Median	108,068	57,235	107,581	8016	55,201	29,886,850	111,974,250	888,260	12,392	4,773,275	100,051	79,471	830,251
	Maximum	116,851	71,674	118,263	11,617	71,400	32,370,000	143,486,500	959,782	15,807	5,101,094	131,704	88,201	998,493
	Minimum	92,949	46,357	88,847	5303	41,319	26,249,125	96,860,000	750,688	9608	4,004,183	54,145	68,380	688,142
	Std. Dev.	6898	7682	6566	1707	9243	1,941,951	13,859,990	61,308	2004	318,287	23,162	6829	96,541
<b>2008q1-2016q2</b>	Mean	105,413	61,098	106,764	7428	50,881	28,606,025	109,446,174	859,991	11,630	4,629,840	87,249	75,840	795,157
	Median	106,199	63,177	107,370	7784	55,016	28,465,413	107,961,550	864,840	11,277	4,689,304	87,129	74,697	798,841
	Maximum	116,851	71,674	118,263	9437	62,840	30,828,500	126,793,800	959,782	14,309	5,101,094	116,805	85,674	904,602
	Minimum	92,949	46,357	88,847	5303	41,319	26,249,125	96,860,000	750,688	9608	4,004,183	54,145	68,380	688,142
	Std. Dev.	7706	7033	7514	1038	6323	1,642,640	7,498,031	60,335	1496	343,765	19,922	5348	71,711
<b>2016q3-2019q2</b>	Mean	108,692	50,484	108,112	10,568	67,469	31,553,327	136,602,817	932,081	15,055	4,840,344	120,957	87,233	959,223
	Median	109,518	50,355	107,822	10,684	67,928	31,601,550	136,396,650	933,147	15,217	4,833,053	121,003	87,275	963,451
	Maximum	111,761	52,913	111,535	11,617	71,400	32,370,000	143,486,500	956,392	15,807	5,064,842	131,704	88,201	998,493
	Minimum	102,662	48,719	104,115	9318	62,816	30,532,050	129,553,500	895,955	14,361	4,501,258	101,797	86,302	910,840
	Std. Dev.	2801	1477	2352	864	2775	573,171	4,748,571	16,280	514	155,509	9376	580	31,561
Panel E: real exports, all figures in million local currencies														
<b>Period</b>		AUSTRALIA	BRAZIL	CANADA	INDIA	ISRAEL	JAPAN	KOREA	MEXICO	NEW ZEALAND	RUSSIA	TURKEY	UNITED KINGDOM	UNITED STATES
<b>2008q1-2019q2</b>	Mean	79,107	36,604	145,090	5663	89,418	19,728,709	164,840,800	1,322,828	15,687	5,190,887	76,892	133,646	557,055
	Median	76,266	36,119	142,094	5952	91,252	19,773,225	175,408,250	1,289,917	15,196	5,119,064	77,290	132,148	572,932
	Maximum	102,453	43,876	169,349	7613	105,119	23,526,475	198,282,100	1,749,114	18,676	6,195,430	105,590	153,660	639,979
	Minimum	62,100	29,652	116,652	3688	67,006	12,862,175	117,732,100	838,697	13,237	4,281,682	52,718	112,494	425,683

Table 13 (continued)

Std. Dev.	13,275	3552	14,218	1089	8736	2,442,964	24,977,141	254,653	1603	528,597	15,565	11,450	60,441
<b>2008q1-2016q2</b>	Mean	35,093	139,203	5260	86,283	18,680,360	156,293,226	1,210,634	14,954	4,931,521	70,221	128,410	534,323
	Median	35,434	139,000	5485	89,572	18,802,688	164,532,900	1,246,730	14,821	4,888,753	71,522	129,361	545,090
	Maximum	90,341	159,638	6586	95,234	21,093,200	183,340,400	1,503,511	17,346	5,497,113	85,687	142,154	600,073
	Minimum	62,100	29,652	3688	67,006	12,862,175	117,732,100	838,697	13,237	4,281,682	52,718	112,494	425,683
Std. Dev.	8780	2637	11,556	941	7619	1,903,686	23,520,782	193,099	1134	319,392	11,534	8017	53,517
<b>2016q3-2019q2</b>	Mean	108,692	50,484	108,112	67,469	31,553,327	136,602,817	932,081	15,055	4,840,344	120,957	87,233	959,223
	Median	109,518	50,355	107,822	67,928	31,601,550	136,396,650	933,147	15,217	4,833,053	121,003	87,275	963,451
	Maximum	111,761	52,913	111,535	71,400	32,370,000	143,486,500	956,392	15,807	5,064,842	131,704	88,201	998,493
	Minimum	102,662	48,719	104,115	62,816	30,532,050	129,553,500	895,955	14,361	4,501,258	101,797	86,302	910,840
Std. Dev.	2801	1477	2352	864	2775	573,171	4,748,571	16,280	514	155,509	9376	580	31,561

Data source: OECD database, Quarterly National Accounts

**Table 14** *P* value of the Phillips-Perron unit root tests for levels and first differences

Country	Real GDP growth rate in %		Real GDP		Real priv. Consumption		Real GFCF		Real exports	
	Level	First difference	Level	First difference	Level	First difference	Level	First difference	Level	First difference
AUSTRALIA	0.0259	-	0.8810	0.0000	0.5564	0.0000	0.6016	0.0060	0.8315	0.0000
BRAZIL	0.0363	-	0.9713	0.0014	0.9417	0.0023	0.3579	0.0010	0.6908	0.0000
CANADA	0.0839	-	0.0012	0.0050	0.0512	0.0101	0.5224	0.0043	0.6873	0.0000
CHINA	0.0993	-	-	-	-	-	-	-	-	-
INDIA	0.0457	-	0.7911	0.0002	0.5175	0.0000	0.8967	0.0346	0.8961	0.0000
ISRAEL	0.0329	-	0.3478	0.0026	0.9514	0.0000	0.6141	0.0097	0.9958	0.0000
JAPAN	0.0080	-	0.6395	0.0000	0.5754	0.0000	0.6123	0.0002	0.0401	0.0001
KOREA	0.0288	-	0.5061	0.0000	0.7796	0.0000	0.3091	0.0135	0.3141	0.0000
MEXICO	0.0315	-	0.0265	0.0031	0.0006	0.0022	0.8722	0.0019	0.7343	0.0024
NEW ZEALAND	0.2689	-	0.9996	0.0000	0.0056	0.0000	0.8674	0.0270	0.8859	0.0000
RUSSIA	0.0013	-	0.6678	0.0046	0.9255	0.0163	0.0993	0.0986	0.3034	0.0000
TURKEY	0.0500	-	0.5621	0.0000	0.4710	0.0000	0.7975	0.3240	0.8735	0.0000
UNITED KINGDOM	0.0353	-	0.4346	0.0764	0.4550	0.0039	0.9035	0.0003	0.2419	0.0000
UNITED STATES	0.1259	-	0.9642	0.0033	0.9982	0.0349	0.5206	0.0214	0.4003	0.0006

**Acknowledgements** I am grateful for the helpful comments, suggestions and criticism of Andre Jungmittag (Frankfurt University of Applied Sciences and DG Joint Research Centre of the European Commission), Paul J.J. Welfens (EIIW/University of Wuppertal), Ronald Schettkat (University of Wuppertal), Tian Xiong (EIIW/University of Wuppertal), participants of the 22nd Annual INFER Conference, participants of the 13th FIW Research Conference in International Economics and seminar participants at the Chair for Macroeconomic Theory and Policy and at the Chair for Economic Policy, University of Wuppertal. I would like to express my sincere thanks to David Hanrahan (EIIW) and Kennet Stave (EIIW) for editorial assistance and also gratefully acknowledge comments and suggestions by two anonymous referees that have significantly helped to improve this paper. Remaining errors are my own.

**Data availability** No

## Declaration

**Conflict of interest** Not applicable.

**Code availability** No

## References

- Abadie A, Gardeazabal J (2003) The economic costs of conflict: a case study of the Basque Country. *Am Econ Rev* 93(1):113–132
- Andrews DWK, Monahan JC (1992) An improved Heteroskedasticity and autocorrelation consistent covariance matrix estimator. *Econometrica* 60:953–966
- Bai J, Ng S (2002) Determining the number of factors in approximate factor models. *Econometrica* 70(1):191–221
- Baier FJ, Welfens PJJ (2018) BREXIT and Foreign Direct Investment: Key Issues and New Empirical Findings. *Int J Financ Stud* 6(46)
- Barro R (2001) Human capital and growth. *Am Econ Rev* 91(2):12–17
- Born B, Müller GJ, Schularick M, Sedláček P (2019) The costs of economic nationalism: evidence from the Brexit experiment. *Econ J* 129(10):2722–2744
- Brakman S, Garretsen H, Kohl T (2017) Consequences of Brexit and options for a "global Britain". CESifo Working Paper Series 6448, CESifo
- Demmou L, Stefanescu I, Arquíe A (2019) Productivity growth and finance: the role of intangible assets - a sector level analysis. OECD Economics Department Working Papers, No. 1547, Paris
- Devereux M, Love D (1994) The effects of factor taxation in a two-sector model of endogenous growth. *Can J Econ* 27(3):509–536
- Dhingra S, Huang H, Ottaviano G, Pessoa JP, Sampson T, Van Reenen J (2017) The costs and benefits of leaving the EU: trade effects. CEP Discussion Paper 1478, Centre for Economic Performance, LSE
- Douch M, Edwards H, Soegaard C (2018) Estimating the trade effects of the Brexit announcement shock. The UK in a Changing Europe Available at: <http://ukandeu.ac.uk/estimating-the-trade-effects-of-the-brexite-announcement-shock/>. Accessed 05 Januar 2020
- Engle RF, Granger CWJ (1987) Co-integration and error correction: representation, estimation, and testing. *Econometrica* 55(2):251–276
- Froot KA, Stein JC (1991) Exchange rates and foreign direct investment: an imperfect capital markets approach. *Q J Econ* 106(4):1191–1217
- Gardeazabal J, Vega-Bayo A (2017) An Empirical Comparison Between the Synthetic Control Method and HSIAO et al.'s Panel Data Approach to Program Evaluation. *J Appl Econ* 32(5):983–1002
- Graziano A, Handley K, Limão N (2018) Brexit uncertainty and trade disintegration. NBER working paper no. 25334, National Bureau of Economic Research
- Grübler J (2017) Wirtschaftliche Konvergenz trotz politischer Unsicherheit. The Vienna Institute for International Economic Studies, Forschungsbericht 7
- Henkel M, Seidel T (2019) A spatial perspective on EUROPEAN integration: heterogeneous welfare and migration effects from the single market and the BREXIT. *Econ Inq* 57(1):333–352

- Hsiao C, Ching HS, Wan SK (2012) A panel data approach for program evaluation: MEASURING the benefits of political and economic integration of Hong KONG with mainland China. *J Appl Econ* 27(5): 705–740
- IMF (2015) Fiscal policy and long-term growth. IMF Policy Paper, USA: International Monetary Fund
- Jungmittag A, Welfens PJJ (2016) Beyond EU-US trade dynamics: TTIP effects related to foreign direct investment and innovation. EIIW Discussion Paper No. 212, European Institute for International Economic Relations, University of Wuppertal
- Ke X, Chen H, Hong Y, Hsiao C (2017) Do China's high-speed-rail projects promote local economy?—new evidence from a panel data approach. *China Econ Rev* 44:203–226
- Korus A, Celebi K (2019) The impact of Brexit news on British pound exchange rates. *Int Econ Econ Policy* 16:161–192
- Li KT, Bell DR (2017) Estimation of average treatment effects with panel data: asymptotic theory and implementation. *J Econ* 197(1):65–75
- Lucas R (1988) On the mechanics of economic development. *J Monet Econ* 22:3–42
- Meinshausen N, Yu B (2009) Lasso-type recovery of sparse representations for high-dimensional data. *Ann Stat* 37(1):246–270
- Newey WK, West KD (1987) A simple, positive semi-definite, Heteroskedasticity and autocorrelation consistent covariance matrix. *Econometrica* 55(3):703–708
- Oberhofer H, Pfaffermayr M (2018) Estimating the trade and welfare effects of Brexit: a panel data structural gravity model. Department of Economics Working Paper Series, 259. WU Vienna University of Economics and Business
- Office for National Statistics (2019) GDP quarterly national accounts, UK: April to June 2019. [Online] Available at: <https://www.ons.gov.uk/economy/grossdomesticproductgdp/bulletins/quarterlynationalaccounts/apriltojune2019>. Accessed 23 December 2019
- Rebello S (1991) Long-run policy analysis and long-run growth. *J Polit Econ* 99(3):500–521
- Serwicka I, Tambari N (2018) Not backing Britain: FDI inflows since the Brexit referendum. Briefing Paper 23, UK Trade Policy Observatory, University of Sussex
- Springford J (2019) CER INSIGHT: The cost of Brexit to June 2019. [online] Available at: [https://www.cer.eu/sites/default/files/insight\\_JS\\_16.10.19.pdf](https://www.cer.eu/sites/default/files/insight_JS_16.10.19.pdf). Accessed 23 December 2019
- Tibshirani R (2011) Regression shrinkage and selection via the lasso: a retrospective. *J R Stat Soc Ser B Methodol* 73(3):273–282
- Wan S, Xie Y, Hsiao C (2018) Panel data approach vs synthetic control method. *Econ Lett* 164:121–123

**Publisher's note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.